



Walther  
Meißner  
Institut

**BAaW**

BAYERISCHE  
AKADEMIE  
DER  
WISSENSCHAFTEN

Technische  
Universität  
München

**TUM**

# Superconductivity and Low Temperature Physics I



**Lecture Notes  
Winter Semester 2022/2023**

**R. Gross  
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# Chapter 1

## Basic Properties of Superconductors

## **1. Basic Properties of Superconductors**



### **1.1 History of Superconductivity**

### **1.2 Perfect Conductivity**

### **1.3 Perfect Diamagnetism**

### **1.4 Type-I and Type-II Superconductors**

### **1.5 Flux Quantization**

### **1.6 Superconducting Materials**

### **1.7 Transition Temperatures**

# 1.1 History of Superconductivity

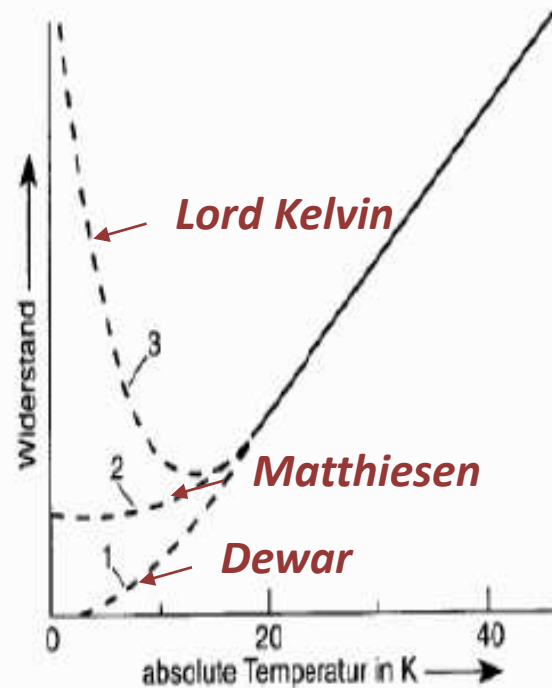
Discovery and explanation of the phenomena of superconductivity and superfluidity was honored by many Nobel Prizes

- 1908 Liquefaction of Helium, 4.2 K ([Kamerlingh Onnes](#))
- 1911 Discovery of zero resistance ([Kamerlingh Onnes](#))
- 1933 Discovery of the Meißner-Ochsenfeld effect ([Meißner & Ochsenfeld](#))
- 1935 London theory ([Fritz & Heinz London](#))
- 1936 type-II superconductivity ([Shubnikov](#))
- 1939 Discovery of superfluid <sup>4</sup>Helium ([Kapitza](#), [Allen](#), and [Misener](#))
- 1952 Ginzburg-Landau theory ([Ginzburg & Landau](#))
- 1957 Abrikosov theory of type-II superconductivity ([Abrikosov](#))
- 1957 Bardeen-Cooper-Schrieffer (BCS) theory ([Bardeen](#), [Cooper](#) & [Schrieffer](#))
- 1961 Discovery of flux quantization ([Doll/Näbauer & Deaver/Fairbank](#))
- 1962 Cooper pair tunneling: Josephson effect ([Josephson](#), [Giaever](#))
- 1966 Development of Superconducting Quantum Interference Devices ([Clarke](#))
- 1971 Discovery of superfluid <sup>3</sup>Helium ([Lee](#), [Richardson](#), [Osheroff](#))
- 1975 Theory of superfluid <sup>3</sup>Helium ([Leggett](#))
- 1979: Discovery of heavy fermion superconductors ([Steglich](#))
- 1981 Discovery of organic superconductors ([Bechgaard](#))
- 1986 Discovery of high-temperature superconductivity ([Bednorz](#), [Müller](#))
- 2006 Discovery of superconductivity in iron pnictides ([Hosono](#))

blue:  
Nobel Prize winners

# 1.1 Discovery of Superconductivity (1911)

- what was the basic interest ?



*temperature dependence of very pure metals  
for  $T \rightarrow 0$  ??*

- $R \rightarrow 0$
- $R \rightarrow \text{const.}$
- $R \rightarrow \infty$

*use of Hg, since very pure Hg was available*

**H. K. Onnes**

*".. Mercury has passed into a new state, which on account of its extraordinary electrical properties may be called the superconductive state"*

# 1.1 Discovery of Superconductivity (1911)

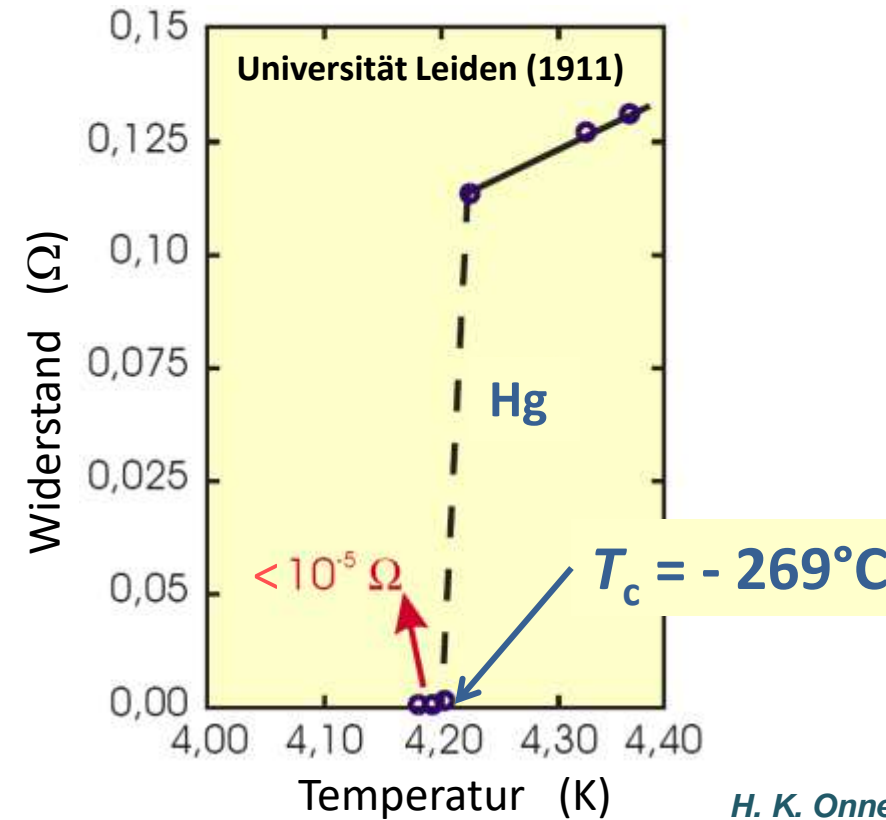
Heike Kamerlingh Onnes (1853-1926)



*note:* Heike = first name, Kamerlingh = „Hofrat“

- Helium liquefaction: 1908
- discovery of superconductivity: 1911

**Nobel Price in Physics 1913**

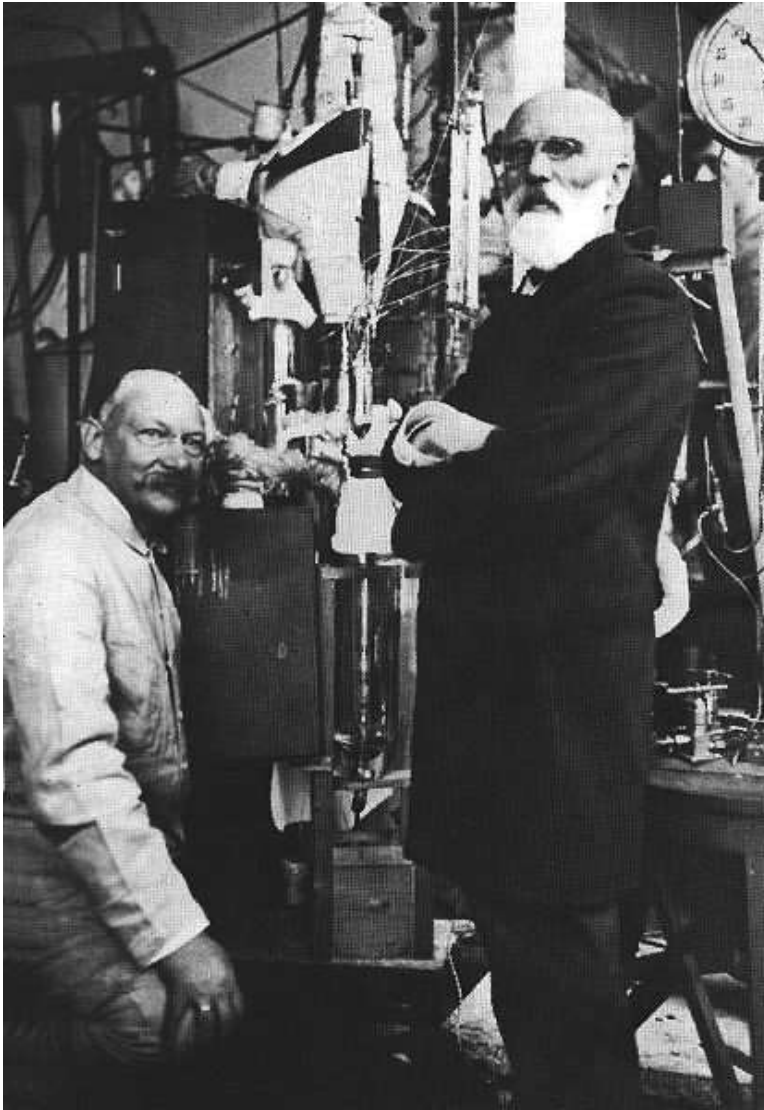


H. K. Onnes,  
Comm. Leiden 120b, 122b, 124c (1911)

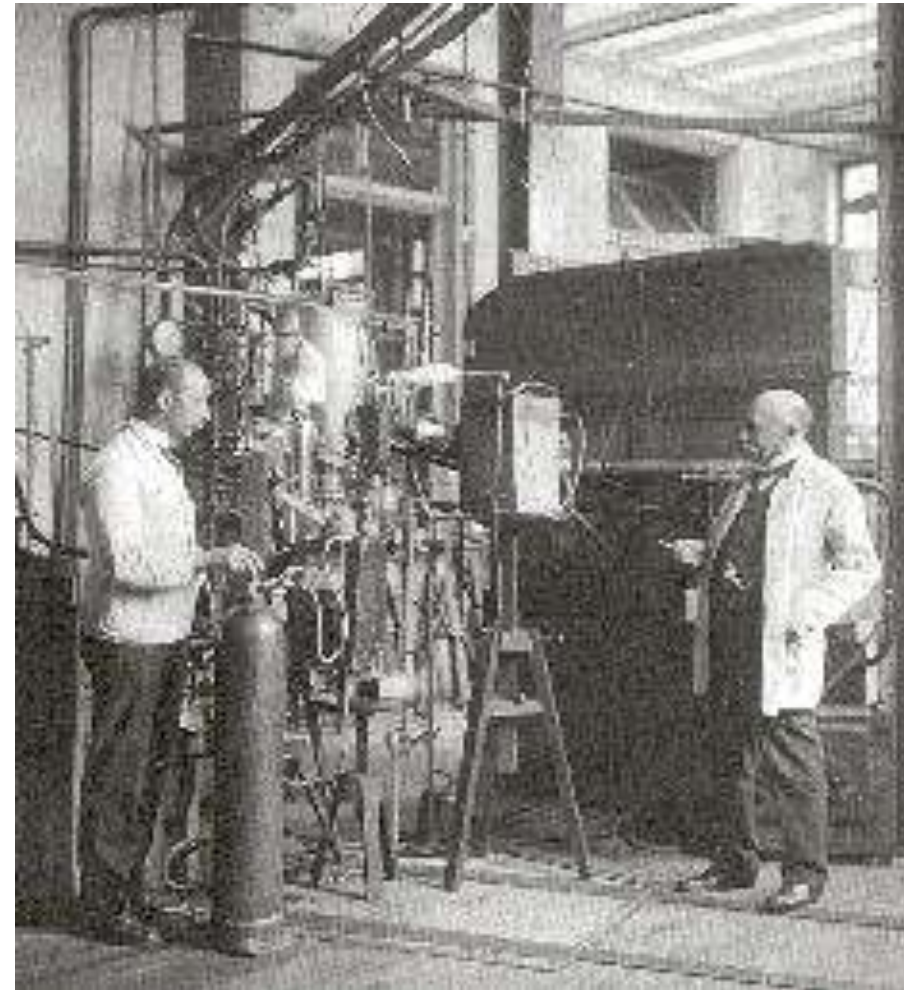
*"for his investigations on the properties of matter at low temperatures which led, inter alia to the production of liquid helium"*

choice of name: *infinite electrical conductivity* → **superconductivity**

# 1.1 Discovery of Superconductivity (1911)



**Kammerlingh Onnes and van der Waals**



**Kammerlingh Onnes and Technician Flim**

# 1.1 Discovery of Superconductivity (1911)



an early picture of the Onnes Laboratory



Kamerlingh Onnes Laboratory, 1924



# 1.1 Discovery of Superconductivity (1911)



**Heike Kamerlingh Onnes** (*far right*) shows his helium liquefactor to three theoretical physicists: Niels Bohr (visiting from Copenhagen), Hendrik Lorentz, and Paul Ehrenfest (*far left*).

# 1.1 Discovery of Superconductivity (1911)



Prof. Heike Kamerlingh Onnes and his wife with some colleagues among them their friend Albert Einstein (*standing behind Mrs. Kamerlingh Onnes*), ca. 1920.

# 1.1 Discovery of the Meißner-Ochsenfeld Effect (1933)

R. Gross and A. Marx, © Walther-Meißner-Institut (2004 - 2022)



**Robert Ochsenfeld**  
(1901 – 1993)



**perfect diamagnetism**

*W. Meißner, R. Ochsenfeld,  
Ein neuer Effekt bei Eintritt der Supraleitfähigkeit,  
Naturwissenschaften 21, 787 (1933).*

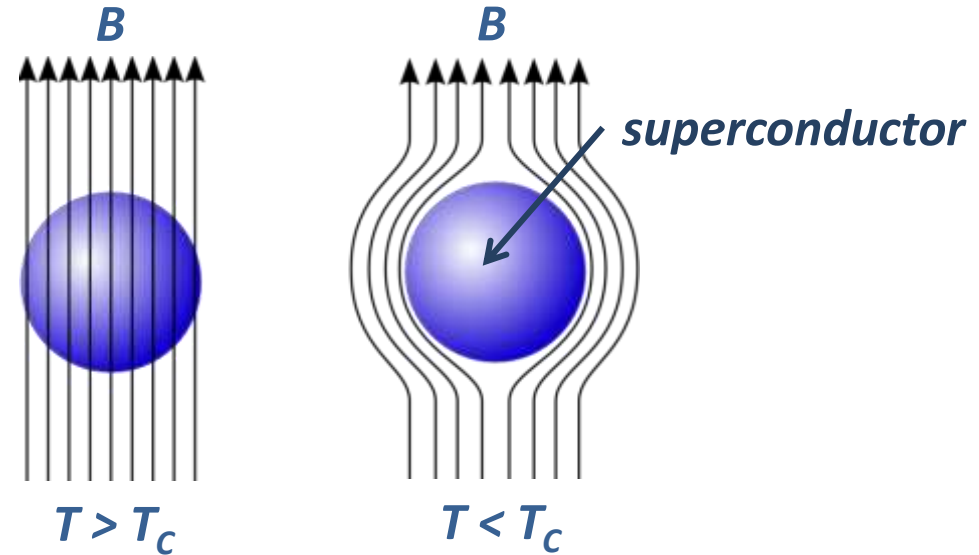


PTB, Institut Berlin

**Walther Meißner**  
(1882 – 1974)

# 1.1 Discovery of the Meißner-Ochsenfeld Effect (1933)

Walther Meißner (1882 – 1974)



superconductors perfectly expel magnetic field

$$B_{\text{in}} = (1 + \chi) B_{\text{ex}} = 0 \quad (\chi = \text{magnetic susceptibility})$$

➔ ideal diamagnetism,  $\chi = -1$

choice of name for perfect diamagnetism:

**Meißner-Ochsenfeld Effect**



# Walther Meißner (1882 – 1974)

- 1913 – 1934** building and heading of low temperature laboratory at the Physikalisch-Technischen-Reichsanstalt, liquefaction of  $H_2$  (20K)
- 7.3.1925** first liquefaction of He in Germany (4.2 K, 200 ml), 3<sup>rd</sup> system world-wide besides Leiden and Toronto
- 1933** discovery of perfect diamagnetism of superconductors together with Ochsenfeld  
→ *Meißner-Ochsenfeld Effect*
- 1934** offer of chair at the Technische Hochschule München (now TUM)
- 1946 – 1950** president of the Bayerischen Akademie der Wissenschaften
- 1946** foundation of the commission for Low Temperature Research  
→ *Walther-Meißner-Institut*



***Walther Meißner***

\* 16. Dezember 1882 in Berlin  
† 15. November 1974 in Munich

## 1935 Fritz and Heinz London

first „quantum mechanical“  
theory of superconductivity  
(*purely phenomenological*)

→ *macroscopic wave function*



**Fritz London**  
**(1900 – 1954)**

**1936 Lev W. Shubnikov**

**discovery of the  
Shubnikov phase in  
superconductors**

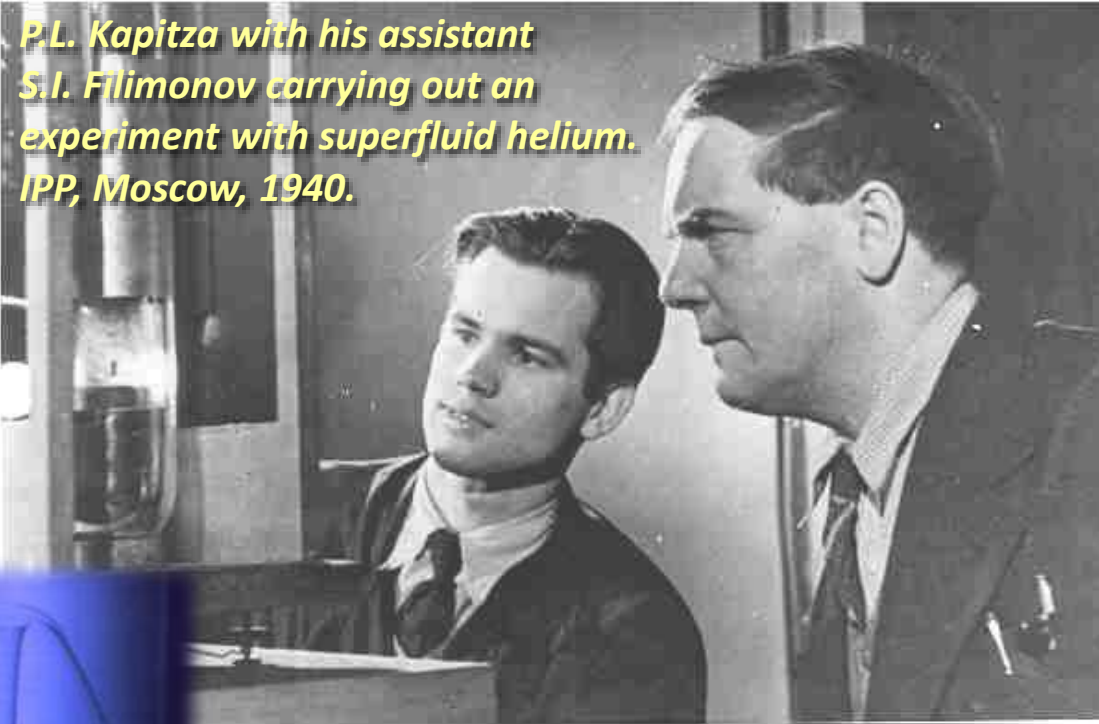
→ *type-I and type-II  
superconductivity*



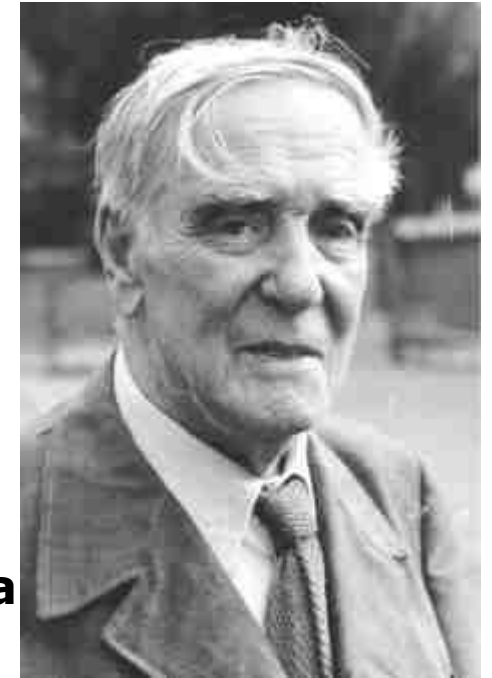
**Lev Wassiljevitsch Shubnikov  
(1901 – 1937)**

# Discovery of Superfluid $^4\text{He}$ (1939)

*P.L. Kapitza with his assistant S.I. Filimonov carrying out an experiment with superfluid helium. IPP, Moscow, 1940.*



*phenomenon analogous to superconductivity is found in an uncharged system*



**Pyotr Leonidovich Kapitza (1894-1984)**



**Nobel Prize in Physics 1978**

*„for his basic inventions and discoveries in the area of low-temperature physics“*



# Ginzburg-Landau Theory (1952)



**Lev Landau**



**Vitaly Ginzburg**

*application of Landau's theory for phase transitions to superconductors using a **complex order parameter***

**Lev Davidovich Landau**

**Nobel Prize in Physics 1962**

*"for his pioneering theories for condensed matter, especially liquid helium"*

**Vitaly Ginzburg**

**Nobel Prize in Physics 2003**

*"for their pioneering contributions to the theory of superconductors and **superfluids**"*

(together with Alexei Abrikosov and Anthony Leggett)

# Non-local London Theory (1953)



**Sir Alfred Brian Pippard**

7. September 1920 – 21. September 2008

*Pippard observed a dependence of the penetration depth on the purity of a material*

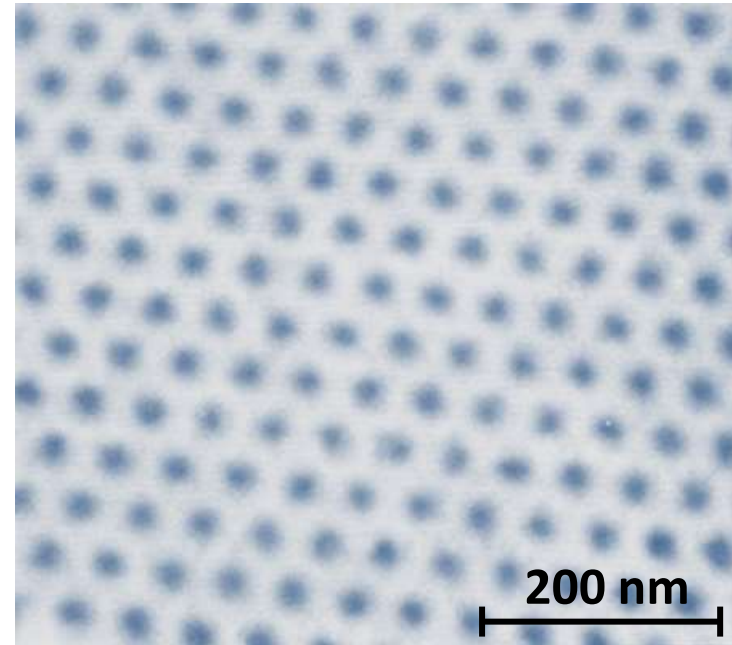
*→ non-local electrodynamics must be used for a proper explanation*

*→ response at position  $r$  depends on the perturbation in a material dependent volume  $\sim |r - \xi_0|^3$*



photo PRB  
**Alexei Abrikosov**

*Abrikosov used the Ginzburg-Landau phenomenology to derive the existence of a “**mixed-state**”*



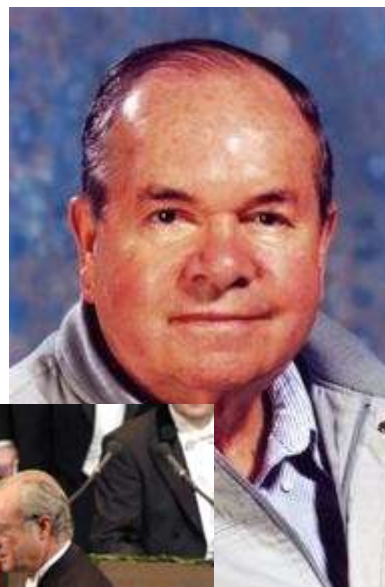
**Alexei Abrikosov**

**Nobel Prize in Physics 2003**

*“for their pioneering contributions to the theory of superconductors and superfluids”*

(together with Vitaly Ginzburg and Anthony Leggett)

# Alexei A. Abrikosov



# The Nobel Prize in Physics 2003



Alexei A. Abrikosov

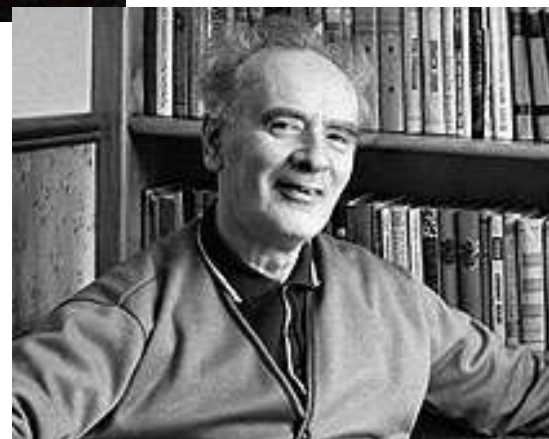
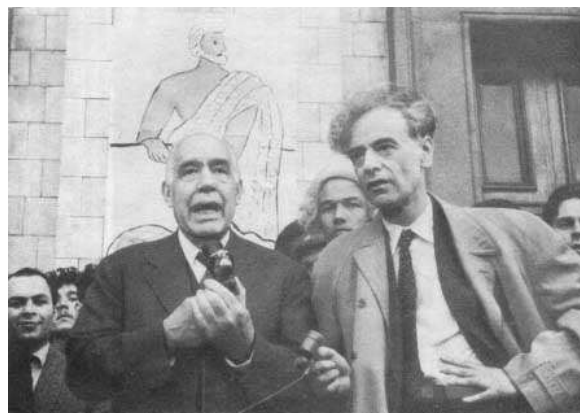
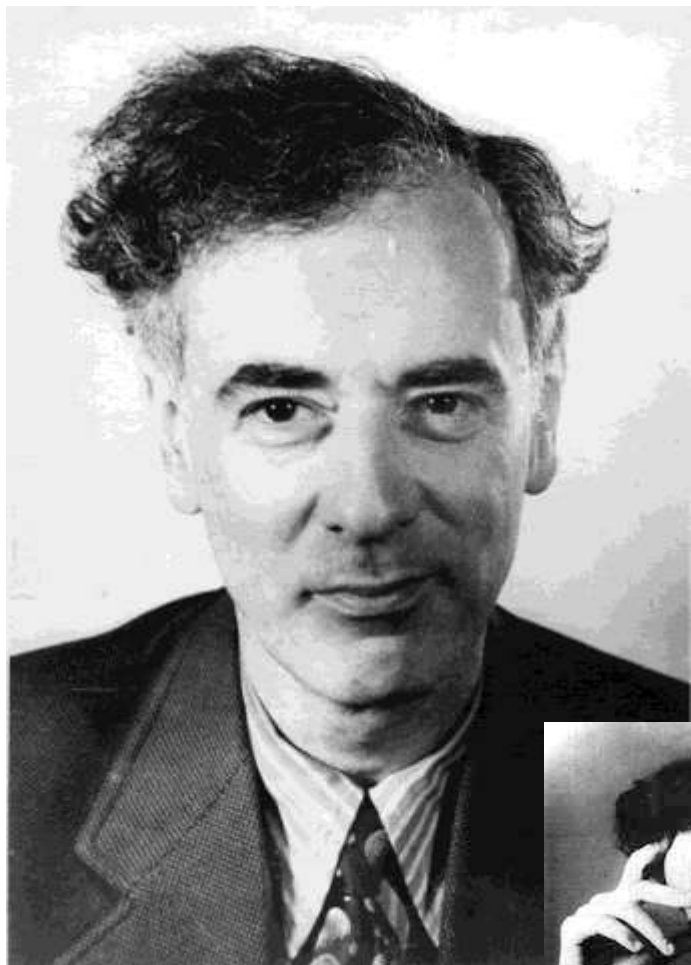


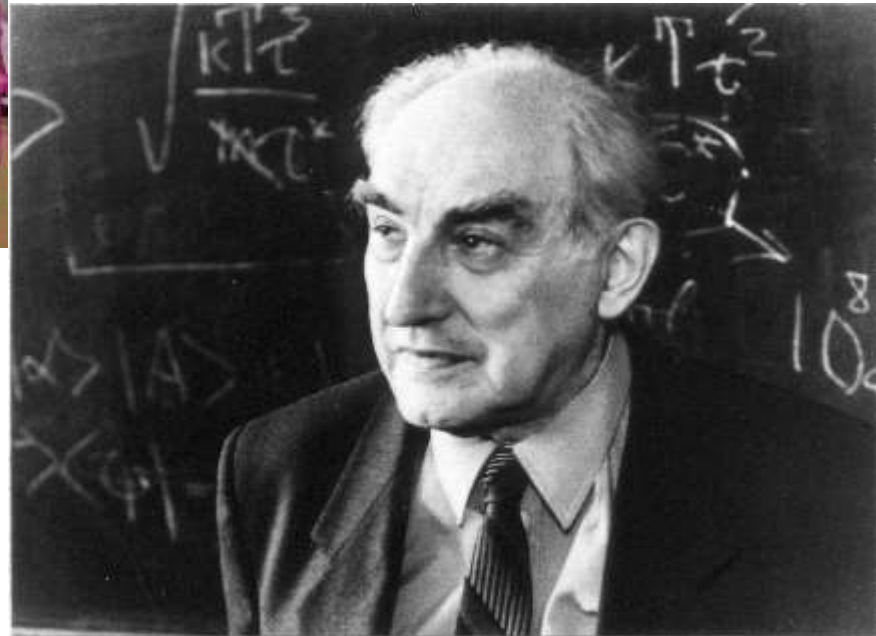
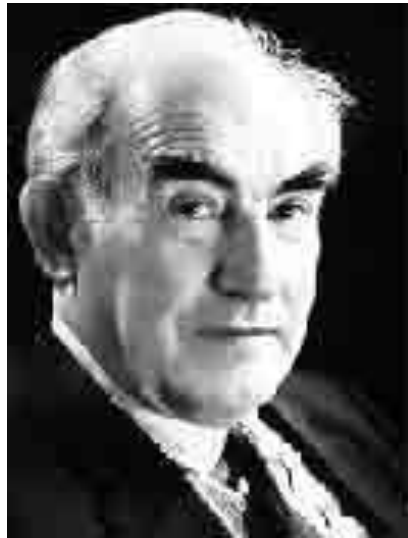
Vitaly L. Ginzburg



Anthony J. Leggett

***..... for their pioneering contributions to the theory of superconductors and superfluids.***







**Tag der Physik**

**07. 07. 2000**



# Microscopic (BCS) Theory (1957)



**J. Bardeen**



**L. N. Cooper**



**R. Schrieffer**

**Nobel Prize in Physics 1972**

*"for their jointly developed theory of superconductivity, usually called the BCS-theory"*

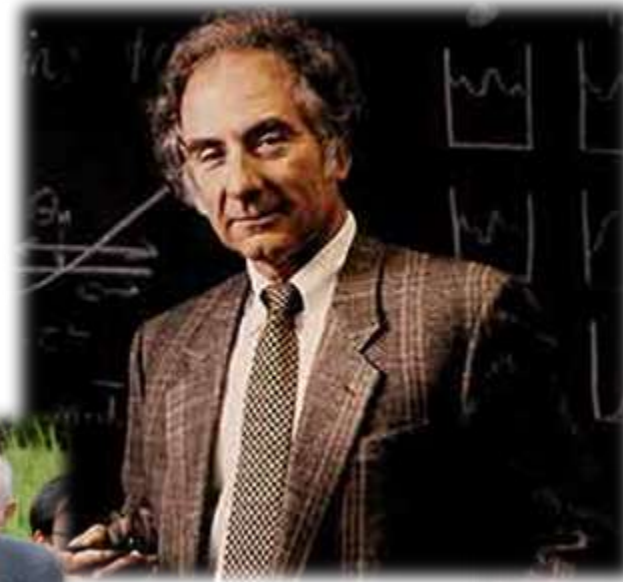
# John Bardeen



\* 23 May 1908, Madison, Wisconsin  
 † 30 January 1991, Boston  
 two-times Nobel Prize winner

# Leon Neil Cooper

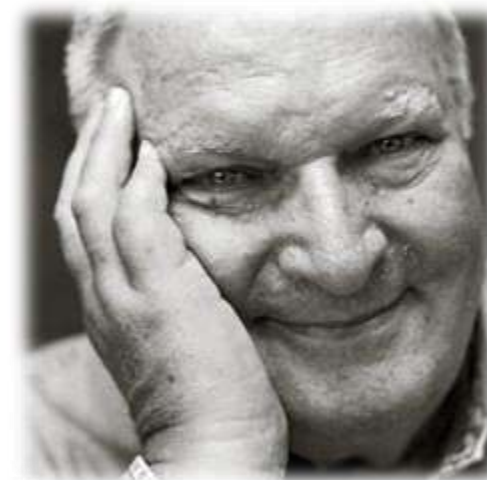
\* 28 February 1930, New York  
Nobel Prize in Physics 1972



Pioneers of superconductivity honored at BCS@50  
From left: Dale J. Van Harlingen, Lev Gor'kov, Charles P. Slichter, Leo Kadanoff, David Pines, Leon Cooper, Marvin Cohen, Michael Tinkham

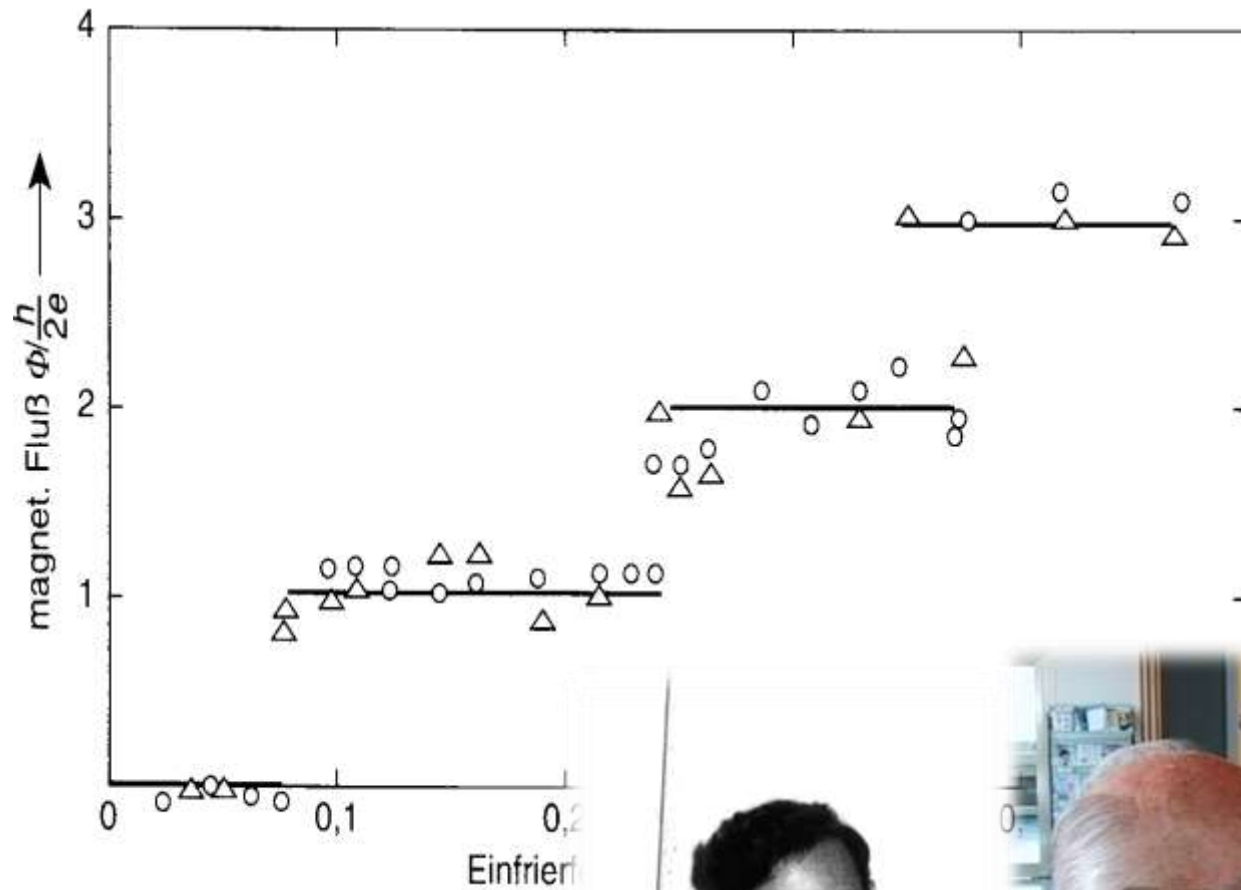
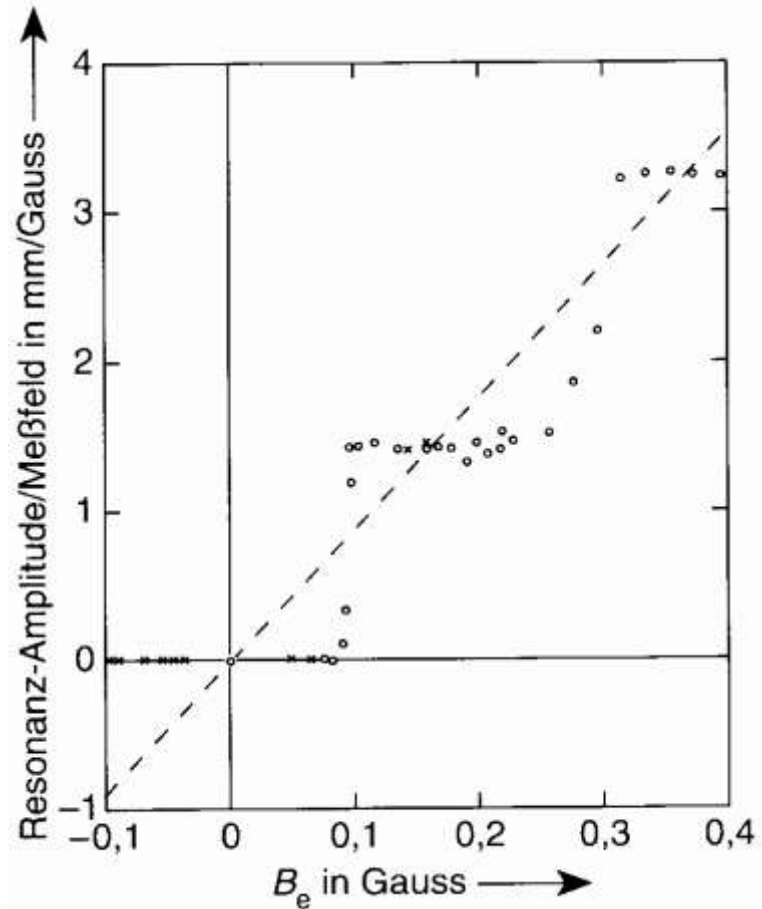


\* 31 May 1931, Oak Park, Illinois  
Nobel Prize in Physics 1972



# Discovery of Flux Quantization (1961)

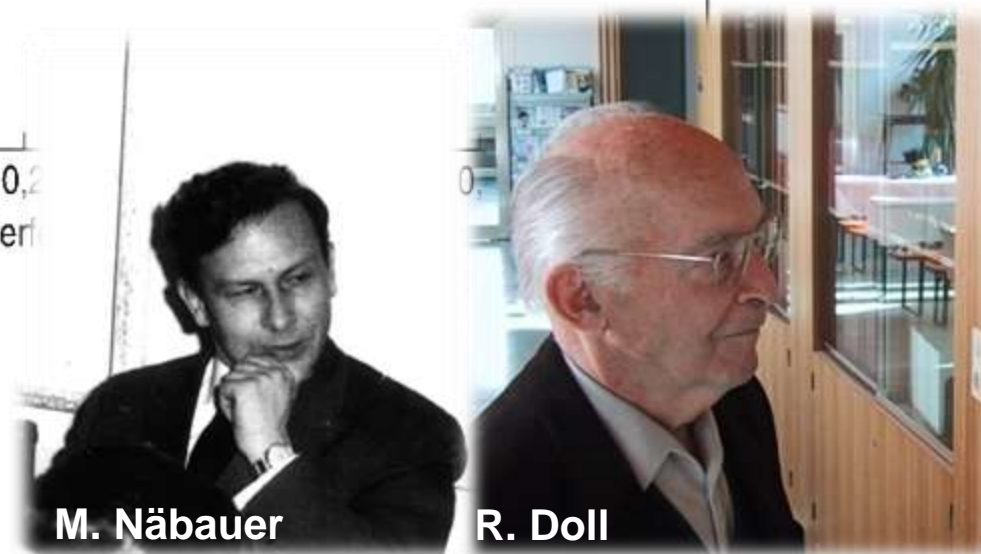
R. Gross and A. Marx, © Walther-Meißner-Institut (2004 - 2022)



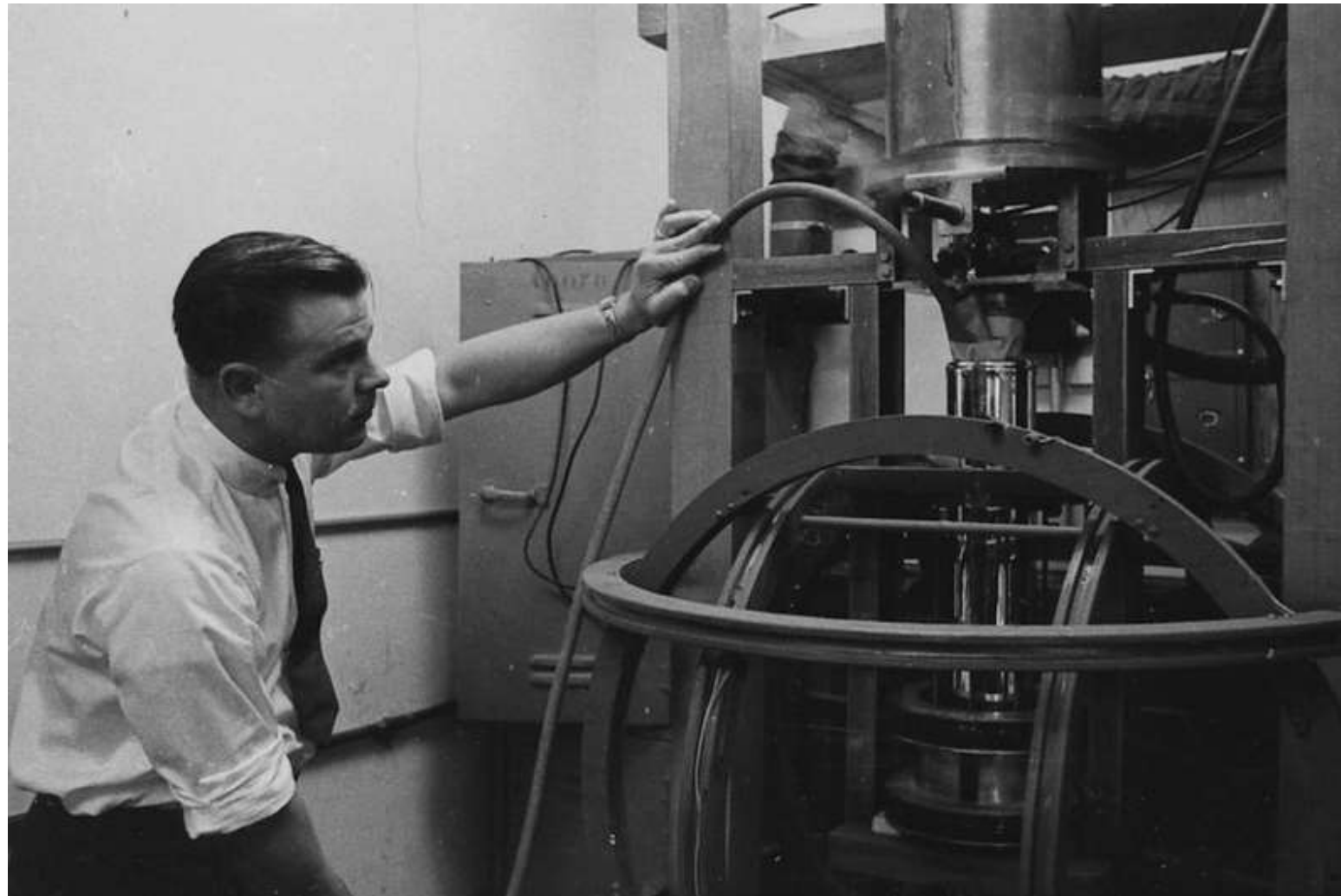
Robert Doll and Martin Näbauer, WMI

R. Doll, M. Näbauer, Phys. Rev. Lett. 7, 51 (1961).

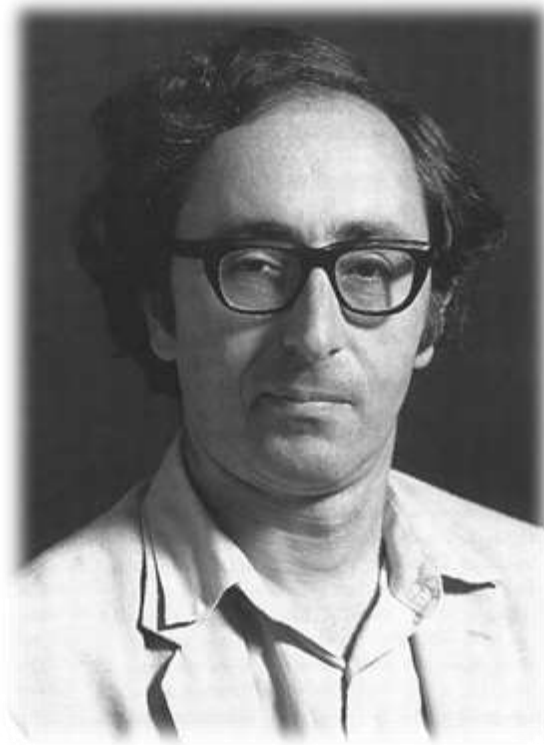
B.S. Deaver Jr., W.M. Fairbank, Phys. Rev. Lett. 7, 43 (1961).



# Discovery of Flux Quantization (1961)



**Measuring the flux quantum.** Graduate student Bascom Deaver refills his apparatus with liquid nitrogen at Stanford University in 1961, a necessary step in maintaining a superconductor at liquid helium temperature. He and William Fairbank used this setup to show that the magnetic field threading a superconducting loop is always quantized. [Credit: J. Mercado/Stanford News Service]



**Brian David Josephson (geb. 1940)**

**Nobel Prize in Physics 1973**

*"for his theoretical predictions of the properties of a supercurrent through a tunnel barrier, in particular those phenomena which are generally known as the Josephson effects"*

(together with Leo Esaki and Ivar Giaever)

# Discovery of Superfluid $^3\text{He}$ (1971/72)



**Douglas D. Osheroff,**  
Stanford University,  
Stanford, California, USA



**David M. Lee,**  
Cornell University, Ithaca,  
New York, USA



**Robert C. Richardson,**  
Cornell University, Ithaca,  
New York, USA

## **Nobel Prize in Physics 1996**

*"for their discovery of superfluidity in helium-3"*

$T_c = 2.6 \text{ mK}$

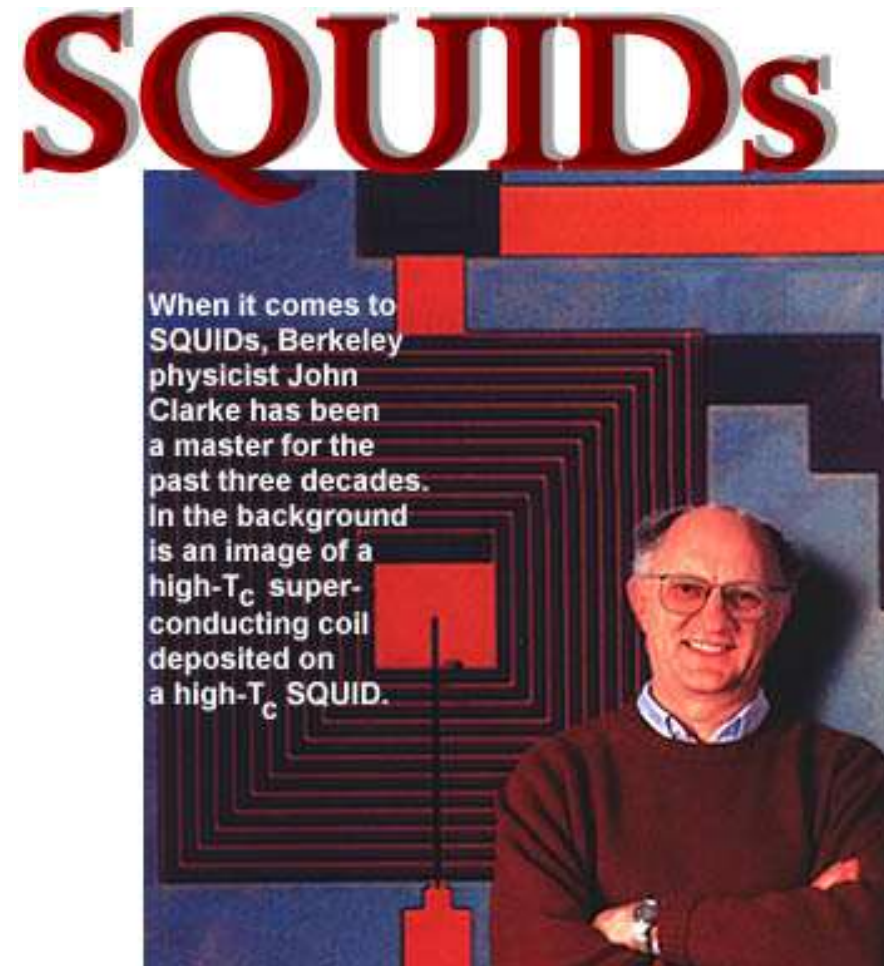
1966  $^3\text{He}/^4\text{He}$  dilution refrigerator: Hall, Neganov **2 mK .... 500 mK**



# Development of SQUID (1966)



**John Clarke**



## Superconducting Quantum Interference Devices



**Anthony J. Leggett**

**Nobel Prize in Physics 2003**

*..... for their pioneering contributions to the theory of superconductors and superfluids.*

(together with Alexey A. Abrikosov and Vitaly Ginzburg)

# Discovery of the High $T_c$ Superconductivity (1986)



**J. Georg Bednorz (b. 1950)    K. Alexander Müller (b. 1927)**

## **Nobel Prize in Physics 1987**

*"for their important break-through in the discovery of superconductivity in ceramic materials"*

# Discovery of the High $T_c$ Superconductivity (1986)



**Karl Alexander Müller**

\* 20. April 1927 in Basel

**Johannes Georg Bednorz**

\* 16. Mai 1950 in Neuenkirchen  
im Kreis Steinfurt

# Summary of Lecture No. 1

- **information on contents and structure of the lectures on superconductivity and low temperature physics I & II**  
**related lectures and seminars**
- **general introduction into the field of low temperature physics**  
**important research fields, related Nobel prizes**  
**information on related research at WMI**
- **A brief history of superconductivity and low temperature physics**  
**important discoveries, key researchers, ....**



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# Superconductivity and Low Temperature Physics I



**Lecture No. 2**

**R. Gross**

**© Walther-Meißner-Institut**

## **1. Basic Properties of Superconductors**

### **1.1 History of Superconductivity**



### **1.2 Perfect Conductivity**

### **1.3 Perfect Diamagnetism**

### **1.4 Type-I and Type-II Superconductors**

### **1.5 Flux Quantization**

### **1.6 Superconducting Materials**

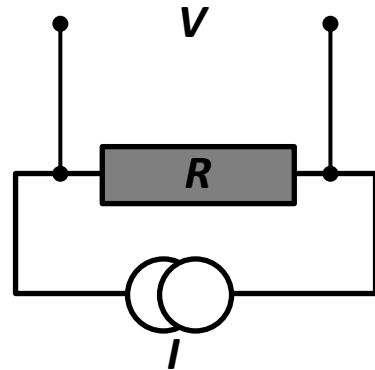
### **1.7 Transition Temperatures**

# 1.2 Perfect Conductivity

- can we measure  $R = 0$  ?

no, only lower threshold  
can be obtained in experiment

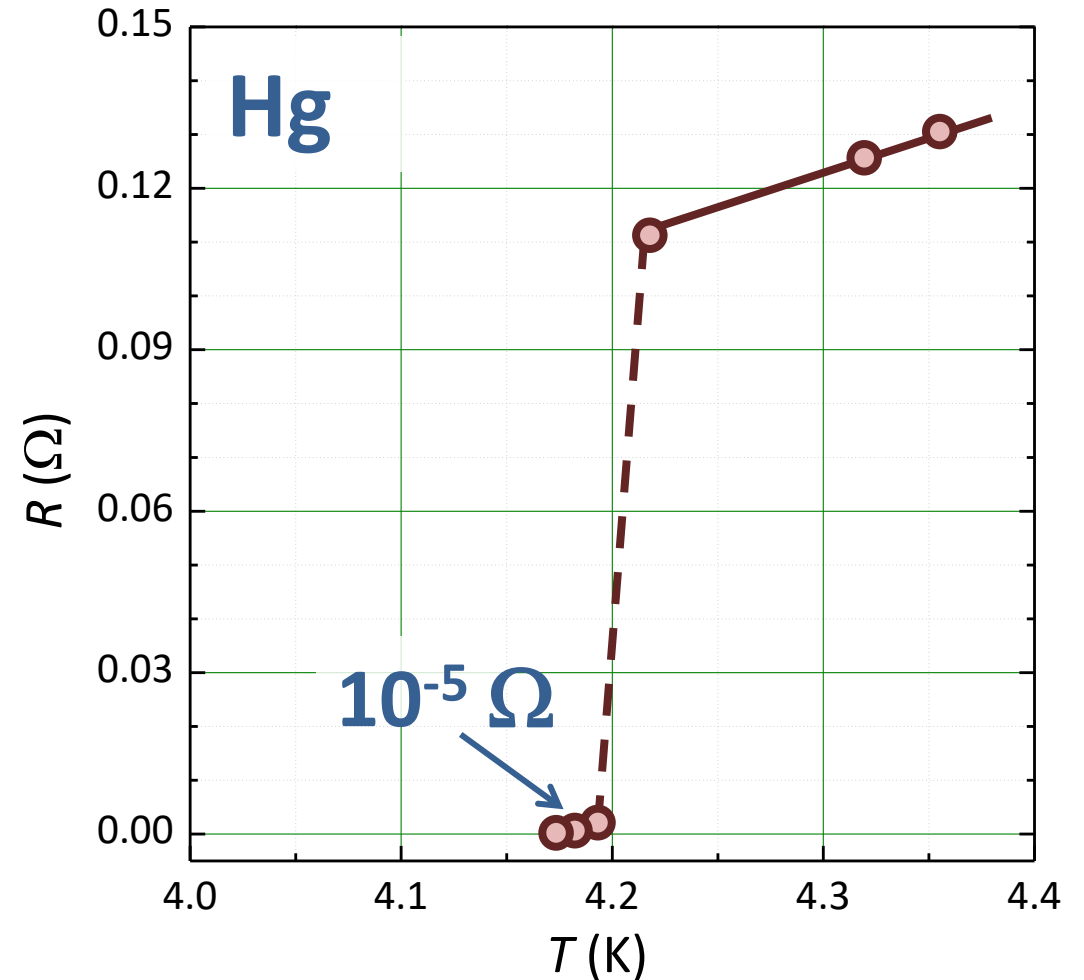
limited resolution of voltage  
measurement



$$\Delta R = \Delta V / I \approx 10^{-8} \Omega$$

@  $\Delta V = 10 \text{ nV}$ ,  $I = 1 \text{ A}$

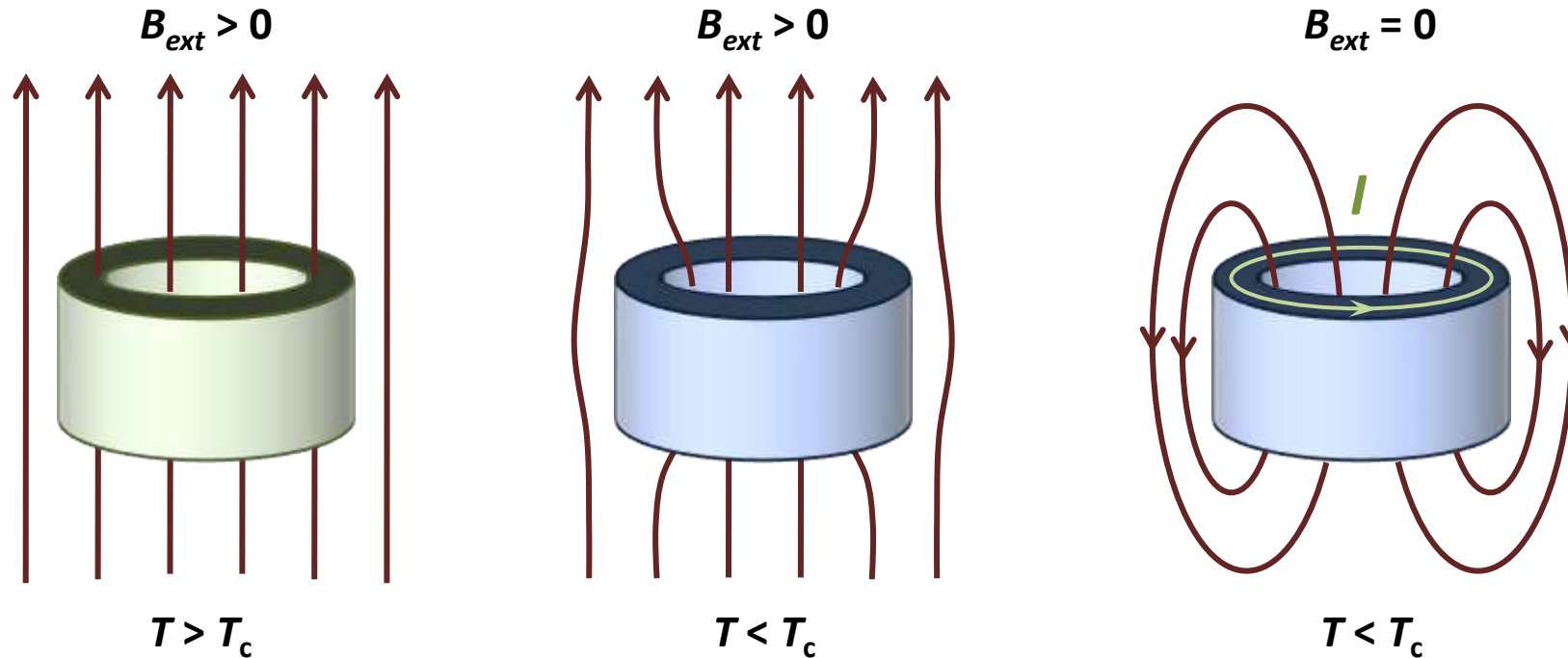
**H. K. Onnes:** resistance drops by about 4 orders of magnitudes (later 14)





# 1.2 Perfect Conductivity

improvement of resistance measurement by study of decay of persistent current



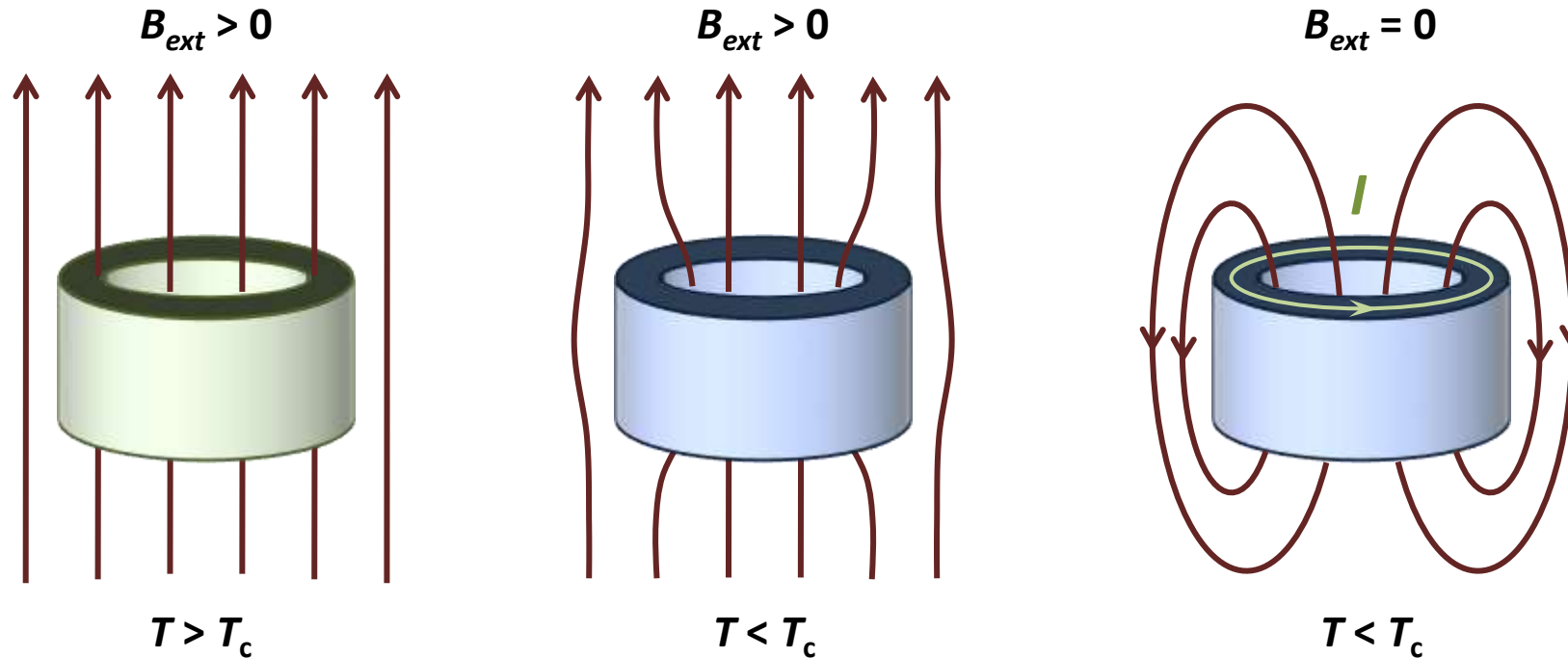
*flux trapping:* Faraday's law:  $-\frac{\partial \mathbf{B}}{\partial t} = \nabla \times \mathbf{E}$

$$-\frac{\partial}{\partial t} \int_A \mathbf{B} \cdot \hat{\mathbf{n}} \, dS = -\frac{\partial}{\partial t} \Phi = \int_A (\nabla \times \mathbf{E}) \cdot \hat{\mathbf{n}} \, dS = \oint_{\Gamma} \mathbf{E} \cdot d\ell = 0$$

*in superconductor (or any perfect conductor):*  $\mathbf{E} = \mathbf{0} \Rightarrow \dot{\Phi} = \mathbf{0} \text{ or } \dot{\mathbf{B}} = \mathbf{0}$

# 1.2 Perfect Conductivity

improvement of resistance measurement by study of decay of persistent current



→ *measure decay of magnetic moment generated by frozen in persistent current*

loop with inductance  $L$  and resistance  $R$ :

$$RI + L \frac{dI}{dt} = 0 \quad \Rightarrow \quad I(t) = I_0 \exp\left(-\frac{R}{L}t\right)$$

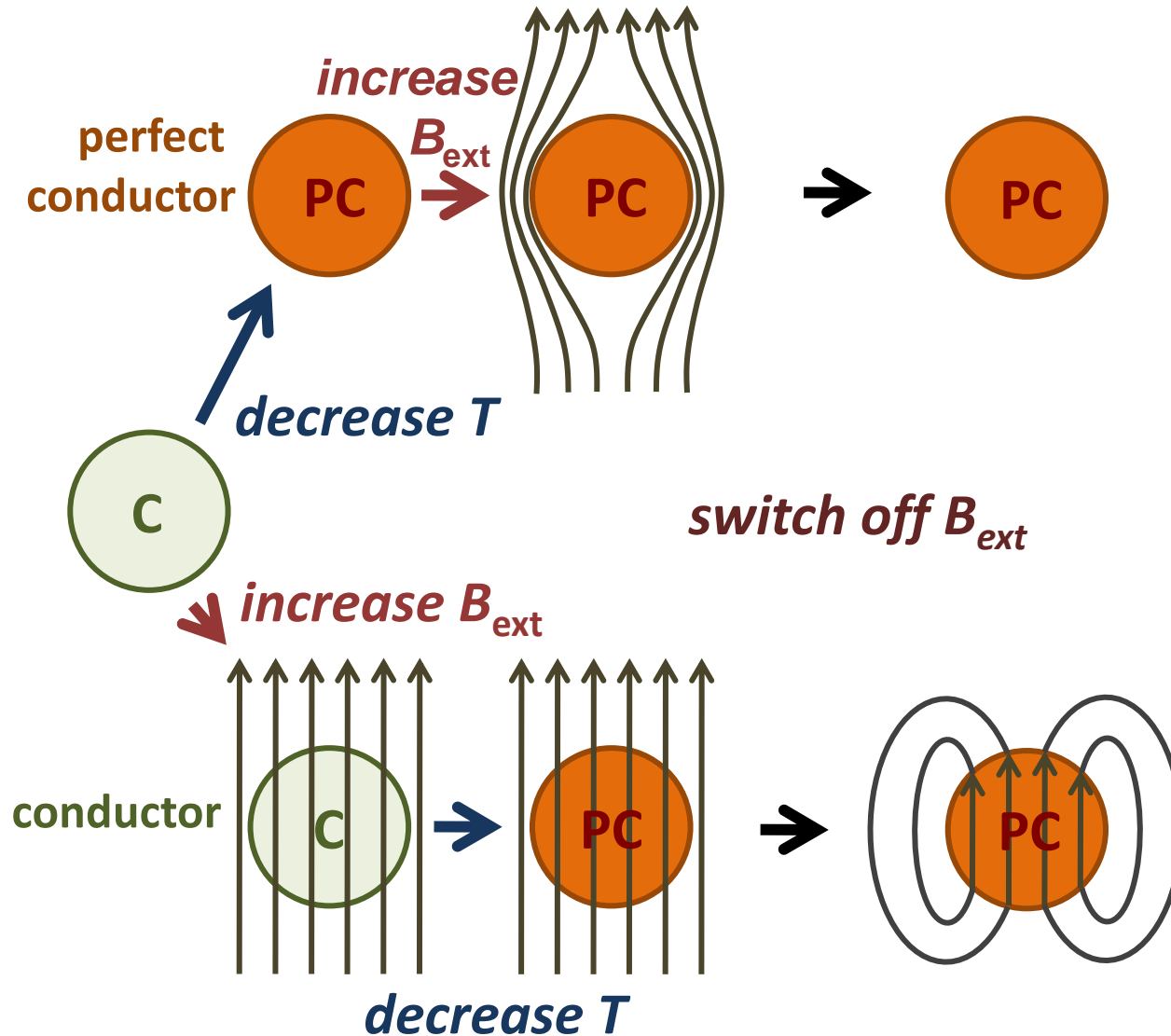
example: 10% decay in 1 year observed

@  $L = 1 \text{ nH}$

→  $R < 10^{-17} \Omega$

# 1.3 Perfect Diamagnetism

perfect conductor in magnetic field



path **dependent**  
final state of the  
perfect conductor

# 1.3 Perfect Diamagnetism

## variation of applied magnetic field for a perfect conductor

*Faraday's law:* 
$$-\frac{\partial \mathbf{B}}{\partial t} = \nabla \times \mathbf{E}$$

*Ohm's law:* 
$$\mathbf{J} = \sigma \mathbf{E} \Rightarrow \mathbf{E} = \frac{\mathbf{J}}{\sigma} = \rho \mathbf{J} = 0$$

↙ = 0 in superconductor

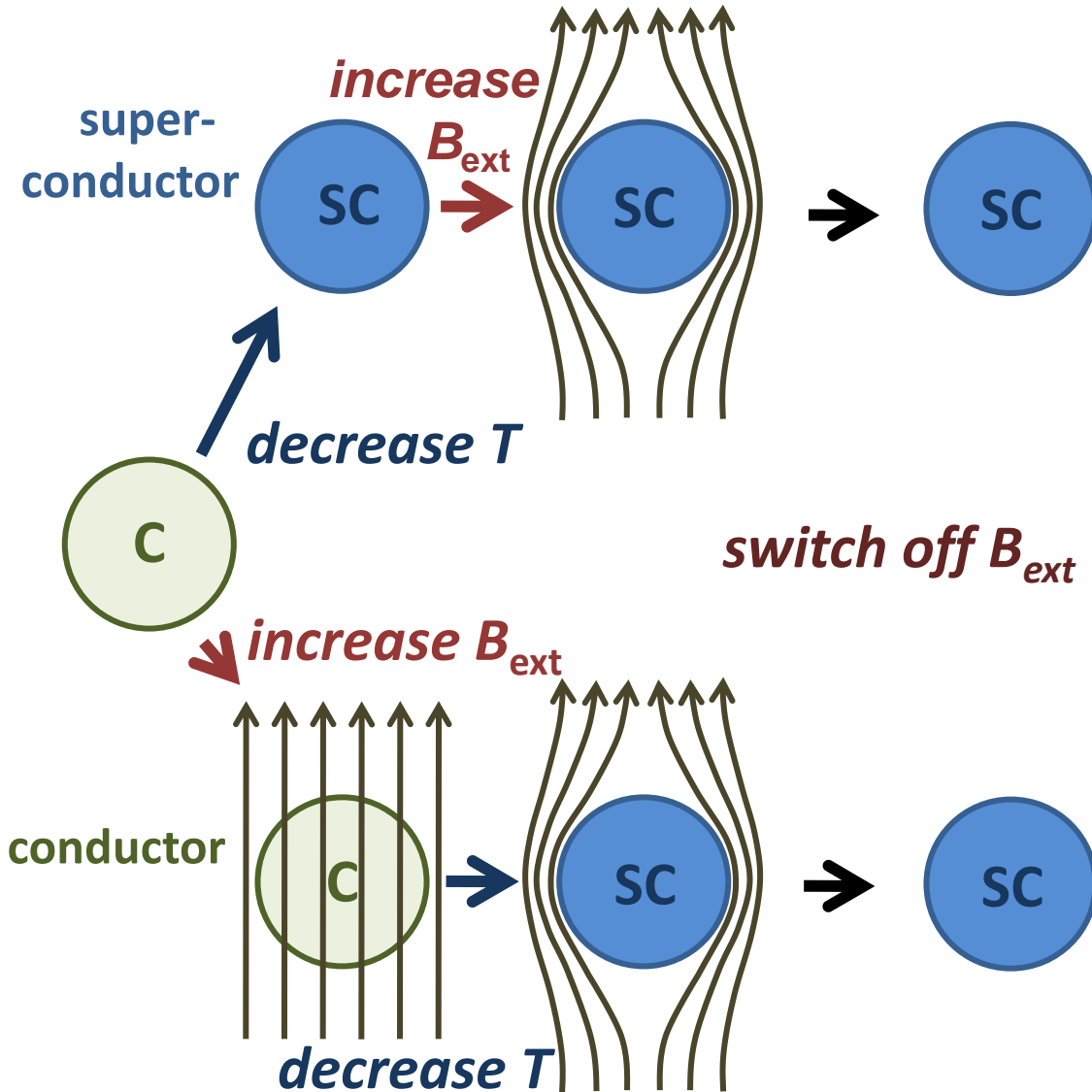
$$\Rightarrow \frac{\partial \mathbf{B}}{\partial t} = 0$$

**→  $B_i = \text{const. inside a perfect conductor}$**

- *field variation → screening currents → shielding of temporal variation of flux density*
- *screening current do not decay →  $B_i = \text{const. forever}$*
- *e.g. flux trapping in ring when switching off external field*

# 1.3 Perfect Diamagnetism

superconductor in magnetic field



path independent  
final state of the  
superconductor

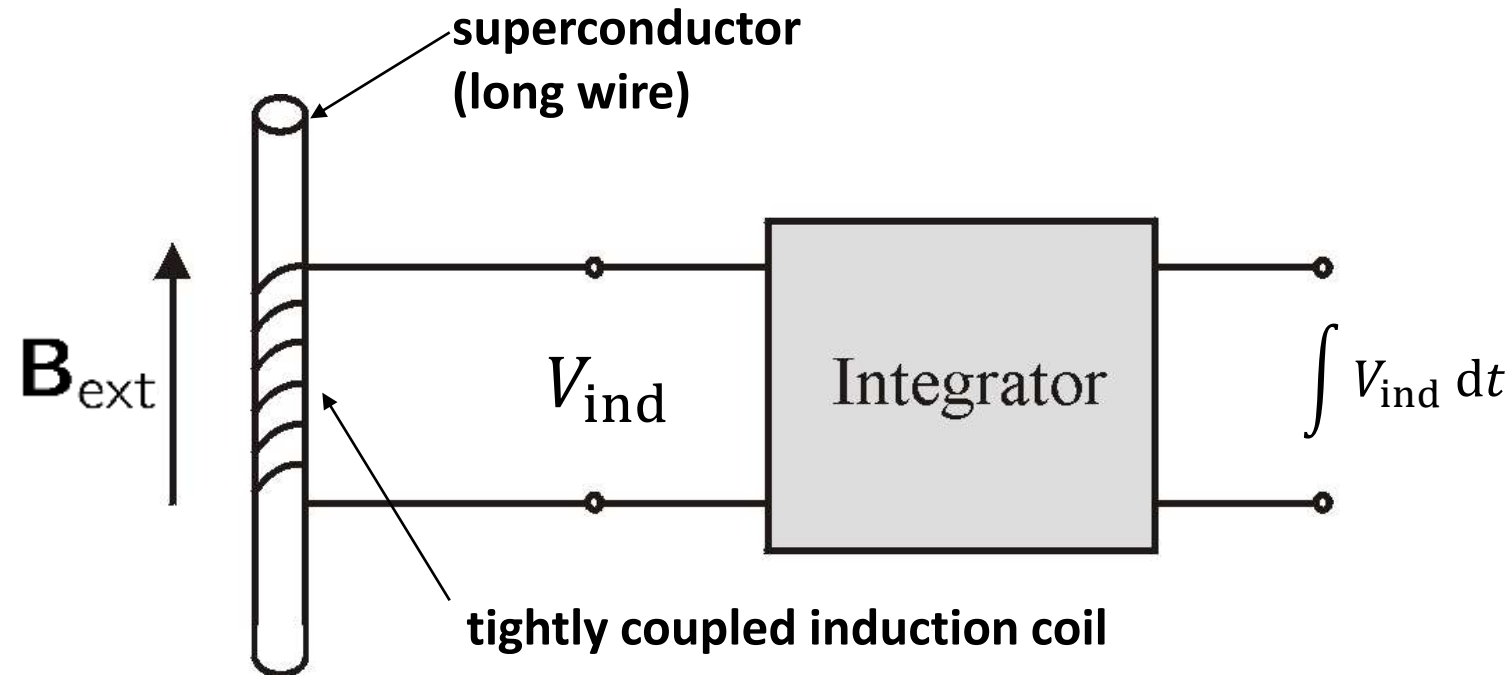


superconducting state is a  
thermodynamic phase

*Meißner-Ochsenfeld-  
Effect*  
or  
*perfect diamagnetism*

# 1.3 Perfect Diamagnetism

simple experimental technique for determination of  $B_i$ :

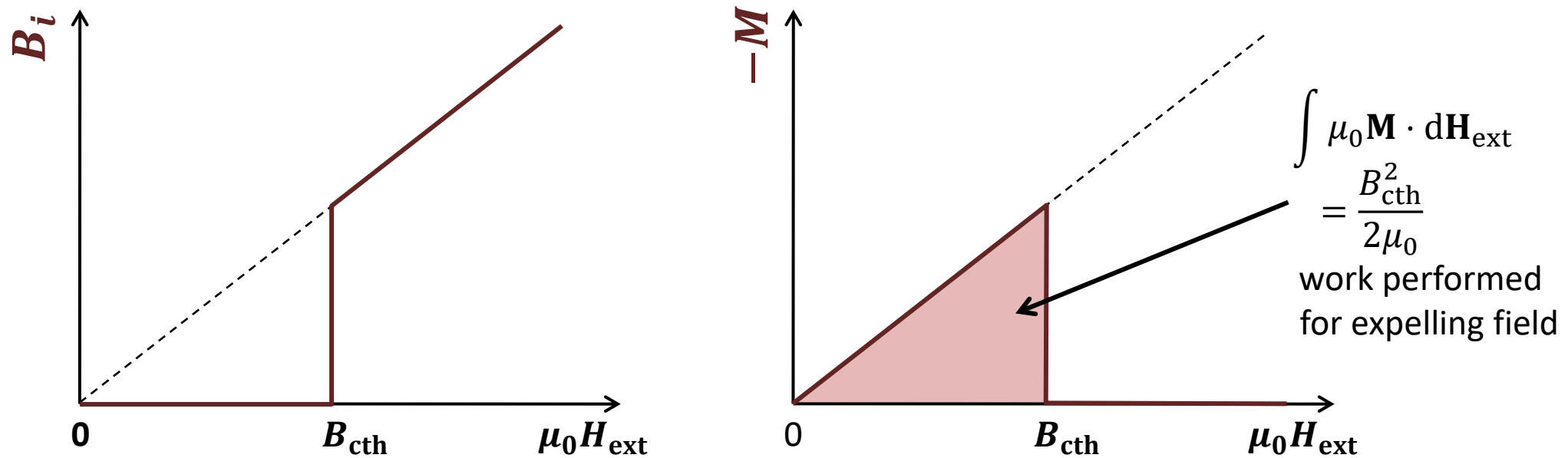


$$V_{\text{ind}} = -\frac{\partial \Phi}{\partial t} \propto -\frac{\partial B_i}{\partial t}$$

$$\Rightarrow \int V_{\text{ind}} dt \propto B_i$$

# 1.3 Perfect Diamagnetism

inner magnetic field  $B_i$  and magnetization  $M$  of superconductors



$$B_i = \mu_0(\mathbf{H}_{\text{ext}} + \mathbf{M}) \quad \chi = -1 \quad \mathbf{M} = B_i/\mu_0 - \mathbf{H}_{\text{ext}}$$

$$\mathbf{M} = \chi \mathbf{H}_{\text{ext}}$$

perfect diamagnetism survives only up to  $T$ -dependent critical field  $B_{\text{cth}}(T)$

- finite energy available for expelling magnetic field
- condensation energy (discussed later)

# 1.3 Perfect Diamagnetism

**observation:** perfect diamagnetism survives only up to  $T$ -dependent critical field  $B_{\text{cth}}(T)$

*interpretation:*

superconductor has only finite amount of energy available for expelling field

$$\frac{B_{\text{cth}}^2(T)}{2\mu_0} = g_n(T) - g_s(T)$$

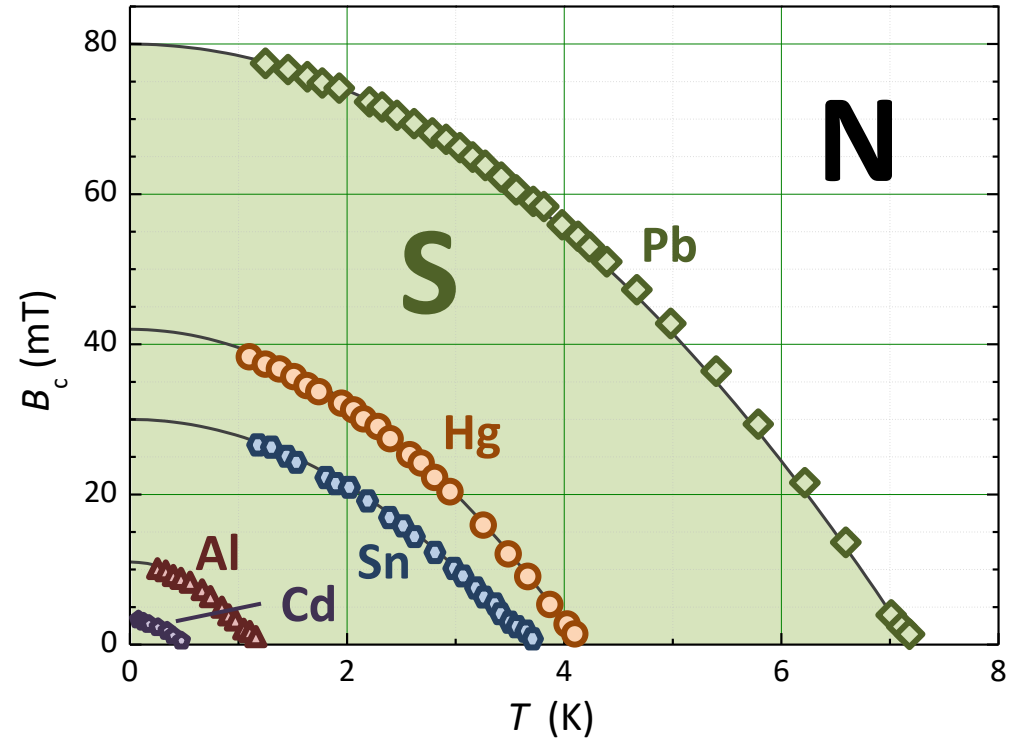
condensation energy

free enthalpy difference of N and S state

*temperature dependence of  $B_{\text{cth}}$ :*

$$B_{\text{cth}}(T) = B_{\text{cth}}(0) \left[ 1 - \left( \frac{T}{T_c} \right)^2 \right]$$

*phase diagram*



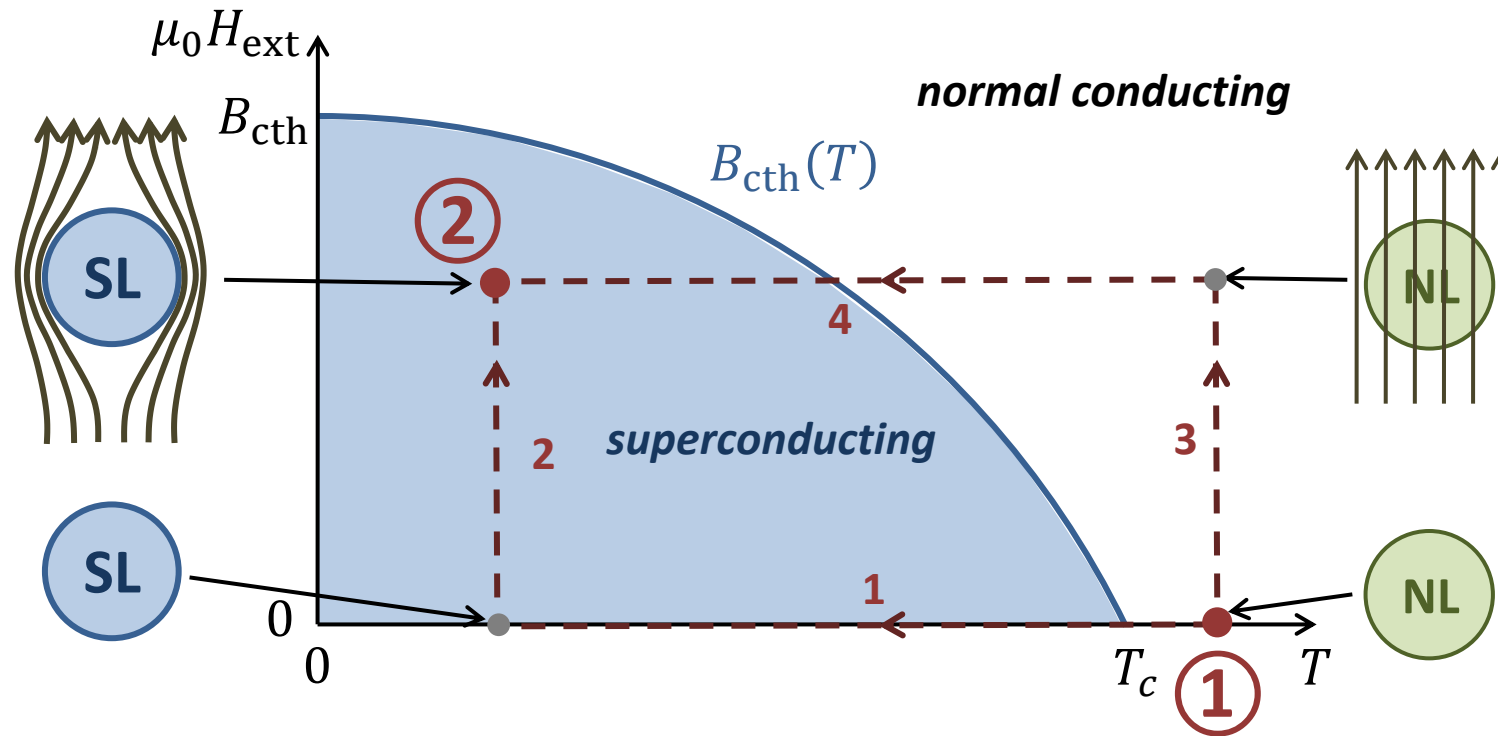
*empirical relation,*

good approximation to exact result of BCS theory



# 1.3 Perfect Diamagnetism

superconductor:  $B_i = 0$  independent of path to position ②



$$B_i = \mu_0(\mathbf{H}_{\text{ext}} + \mathbf{M}) = \mu_0(\mathbf{H}_{\text{ext}} + \chi\mathbf{H}_{\text{ext}}) = \mu_0\mathbf{H}_{\text{ext}}(1 + \chi) = 0$$

→ perfect diamagnetism:  $\chi = -1$

→ superconducting state is *thermodynamic phase*

# 1.3 Perfect Diamagnetism

## Meißner effect:

*path-independent complete exclusion of magnetic flux from the interior of a bulk superconductor*

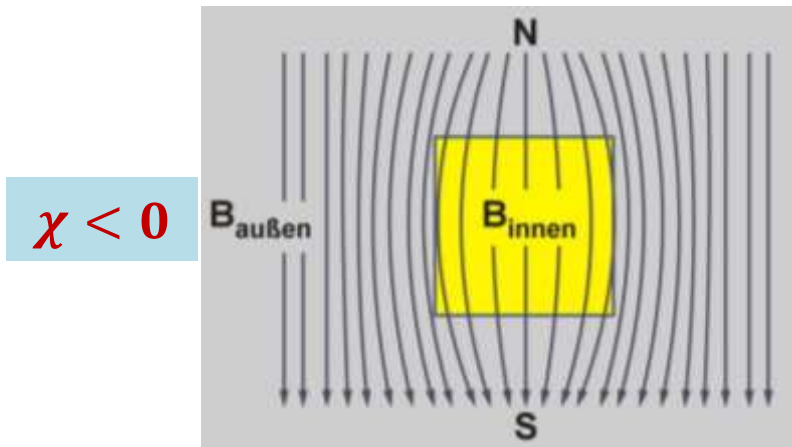
### important remaining questions

- How does the magnetic induction  $B$  change at the surface? Step-like change?
- How do the screening currents set-off if not according to Faraday's law?
- Can the magnetic flux penetrate partially to reduce the magnetic energy?
- What happens in a superconductor that is not simply connected (e.g. superconductor with hole such as a cylinder)?

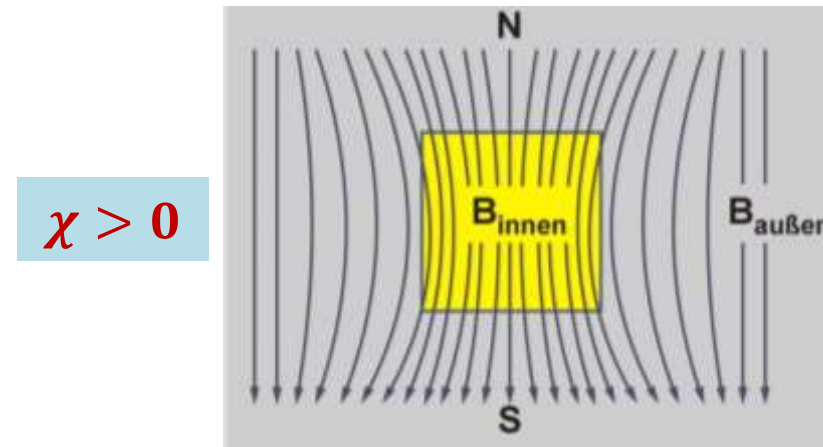
# 1.3 Perfect Diamagnetism

## levitation of diamagnetic materials

*diamagnetic materials*

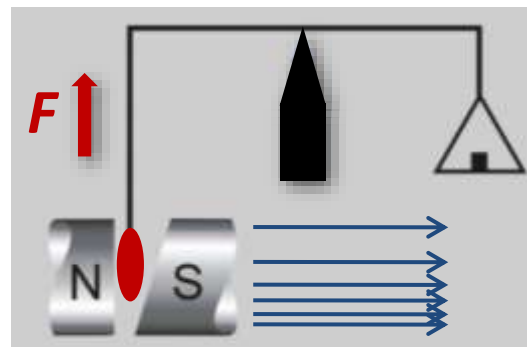


*para- or ferromagnetiv materials*



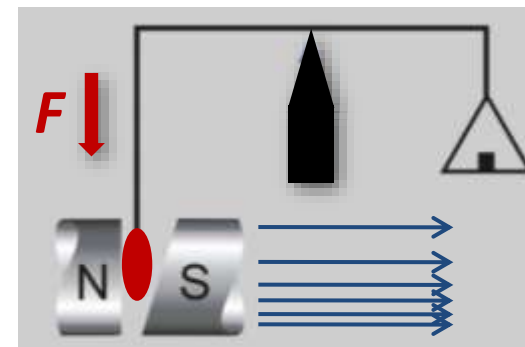
$$\mathbf{B}_i = (1 + \chi) \mu_0 \mathbf{H}_{\text{ext}}$$

( $\chi$  = magnetic susceptibility)



*material becomes „lighter“*

*Faraday balance*



*material becomes „heavier“*

# 1.3 Perfect Diamagnetism

## levitation of diamagnetic materials

$$F_{\text{buoyancy}} = \frac{\chi}{2\mu_0} \mathbf{B} \cdot \nabla \mathbf{B}$$

*magnetic field*
*gradient of magnet field*

*buoyancy = gravity*

$$F_{\text{gravity}} = \rho g$$

*mass density*
*acceleration of gravity: 9.8 m/s<sup>2</sup>*

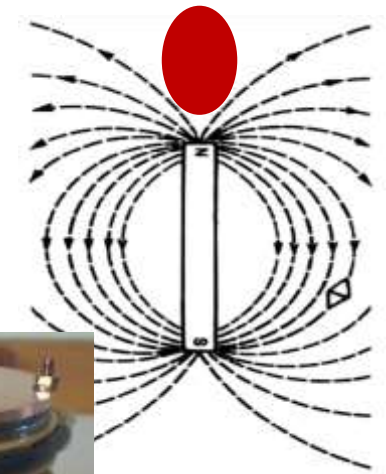
$$\mathbf{B} \cdot \nabla \mathbf{B} \left[ \frac{\text{T}^2}{\text{m}} \right] \approx 0.02 \cdot \frac{\rho [\text{g/cm}^3]}{\chi}$$

- organic materials:*

$$\rho \simeq 1 \text{ g/cm}^3, \chi \simeq -1 \cdot 10^{-5}$$

➔  $\mathbf{B} \cdot \nabla \mathbf{B} \simeq 1\,000 \left[ \frac{\text{T}^2}{\text{m}} \right]$

*can be achieved with strong magnet:  
B = 20 Tesla, grad B = 100 T/m*



10 cm

# Levitated tomatos, strawberries, ....

tomato



source: <http://www.hfml.ru.nl/>

frog



grasshopper



strawberry



water troplet

# 1.3 Perfect Diamagnetism

• *organic materials:*

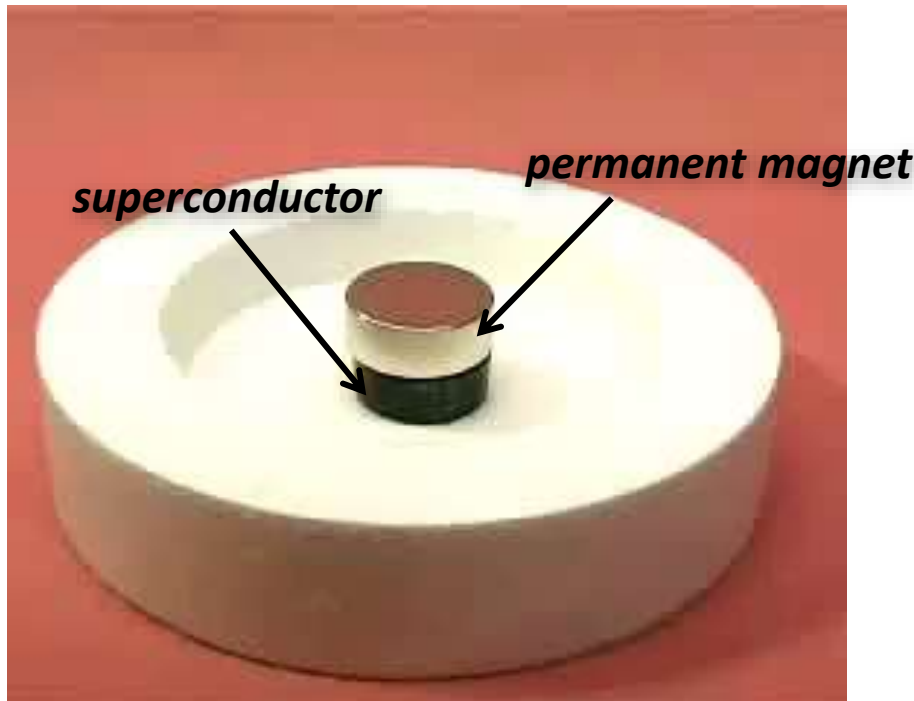
$$\rho \simeq 1 \text{ g/cm}^3, \chi \simeq -1 \cdot 10^{-5}$$

$$\Rightarrow B \cdot \nabla B \simeq 1\,000 \left[ \frac{\text{T}^2}{\text{m}} \right]$$

• *superconductors:*

$$\rho \simeq \text{a few g/cm}^3, \chi \simeq -1$$

$$\Rightarrow B \cdot \nabla B \simeq 0.01 \left[ \frac{\text{T}^2}{\text{m}} \right]$$



**Superconductors:**

*ideal materials for magnetic levitation*

## **1. Basic Properties of Superconductors**

### **1.1 History of Superconductivity**

### **1.2 Perfect Conductivity**

### **1.3 Perfect Diamagnetism**



### **1.4 Type-I and Type-II Superconductors**

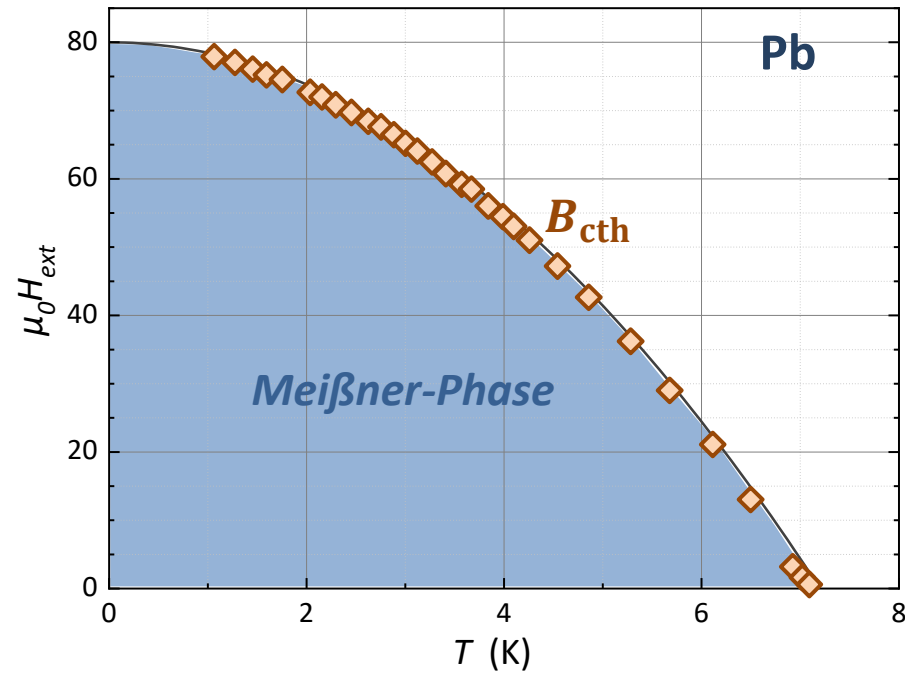
### **1.5 Flux Quantization**

### **1.6 Superconducting Materials**

### **1.7 Transition Temperatures**

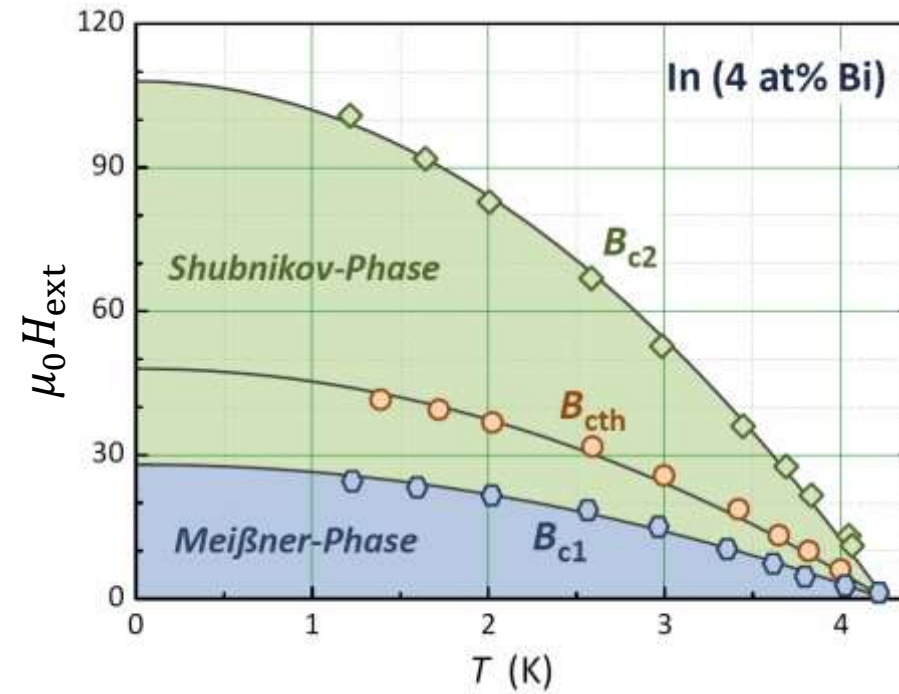
# 1.4 Type-I and Type-II Superconductors

Type-I Superconductor



- Meißner-Phase for  $B_{ext} < B_{cth}$
- no Shubnikov-Phase

Type-II Superconductor



- Meißner-Phase for  $B_{ext} < B_{c1}$
- Shubnikov-Phase for  $B_{c1} < B_{ext} < B_{c2}$

$$B_{c1} < B_{cth} < B_{c2}$$



## **1. Basic Properties of Superconductors**

### **1.1 History of Superconductivity**

### **1.2 Perfect Conductivity**

### **1.3 Perfect Diamagnetism**

### **1.4 Type-I and Type-II Superconductors**



### **1.5 Flux Quantization**

### **1.6 Superconducting Materials**

### **1.7 Transition Temperatures**

# 1.4 Flux Quantization

- discovered 1961 by
  - **Robert Doll** and **Martin Näbauer** (WMI)
  - **B.S. Deaver** and **W.M. Fairbanks** (Stanford University)

- **experiment by Doll and Näbauer (WMI)**

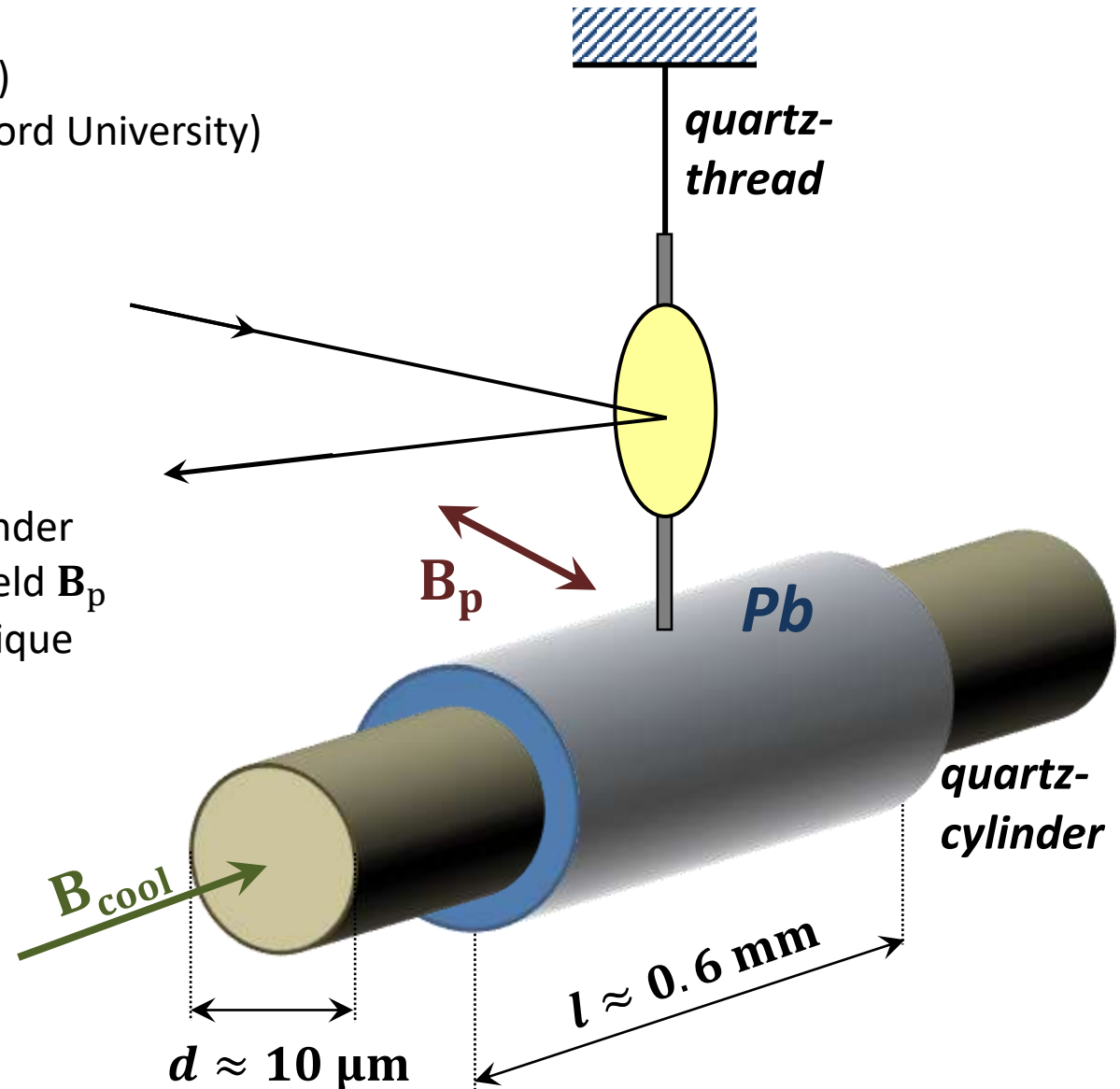
- trapping of magnetic flux in hollow cylinder
- apply torque  $\mathbf{D} = \boldsymbol{\mu} \times \mathbf{B}_p$  by probing field  $\mathbf{B}_p$
- increase sensitivity by resonance technique

- number of trapped flux quanta:

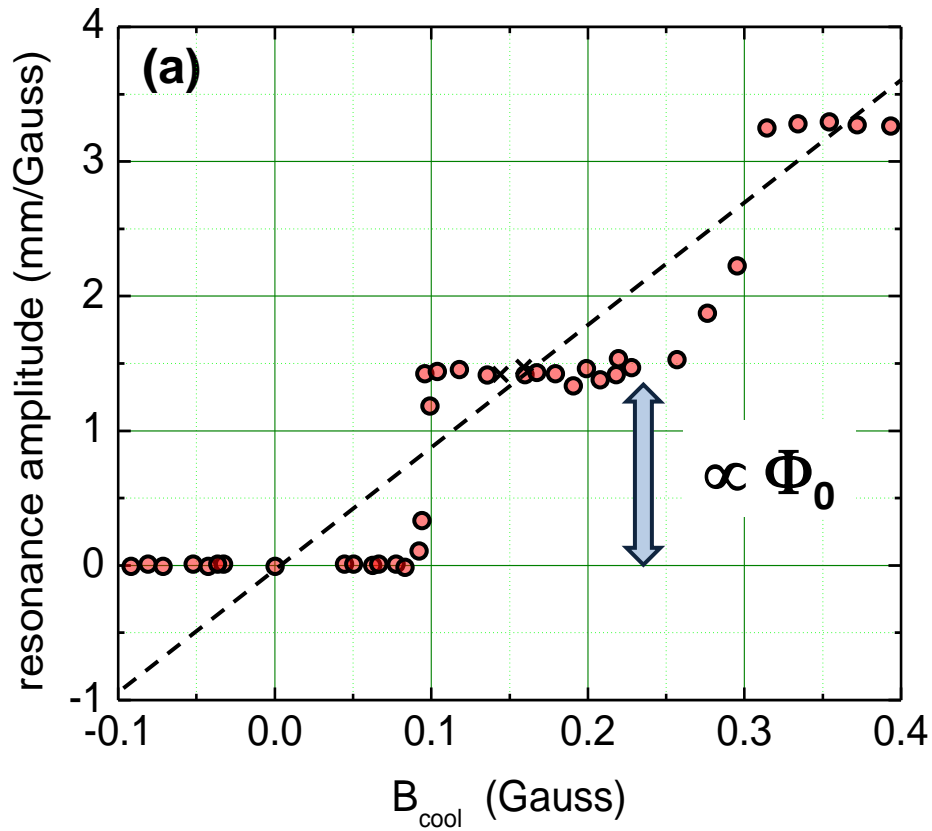
$$N = B_{\text{cool}} \pi (d/2)^2$$

$$N \approx 1$$

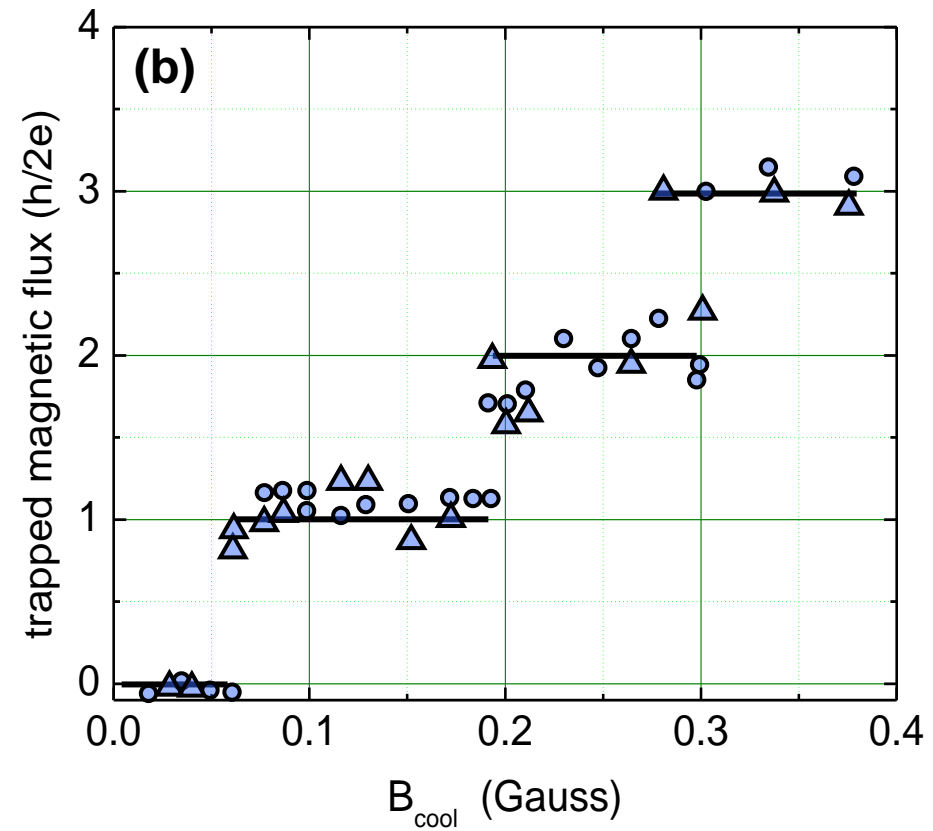
$$\text{@ } B_{\text{cool}} = 10^{-5} \text{ T, } d = 10 \text{ } \mu\text{m}$$



# 1.4 Flux Quantization



**R. Doll, M. Näbauer**  
Phys. Rev. Lett. **7**, 51 (1961)



**B.S. Deaver, W.M. Fairbank**  
Phys. Rev. Lett. **7**, 43 (1961)

$$\Phi_0 = \frac{h}{2e}$$

prediction by F. London:  $h/e$

→ **experimental proof for existence of Cooper pairs**

[Paarweise im Fluss](#)

D. Einzel, R. Gross, Physik Journal 10, No. 6, 45-48 (2011)

## **1. Basic Properties of Superconductors**

### **1.1 History of Superconductivity**

### **1.2 Perfect Conductivity**

### **1.3 Perfect Diamagnetism**

### **1.4 Type-I and Type-II Superconductors**

### **1.5 Flux Quantization**



### **1.6 Superconducting Materials**

### **1.7 Transition Temperatures**

# 1.6 Superconducting Materials

- discovery of superconductivity in chemical element Hg
- since then thousands of further superconducting compounds found
- classification into families:
  1. elemental superconductors (Hg, 1911)
  2. alloys and intermetallic compounds
  3. heavy Fermion superconductors (1979)
  4. organic superconductors (1981)
  5. fullerenes (1991)
  6. oxides superconductors , cuprates (1986)
  7. iron pnictides (2006)

MgB<sub>2</sub> (2001)

# 1.6 Superconducting Materials

<sup>1</sup> H	<i>superconducting @ p = 1 bar</i>																<sup>2</sup> He						
<sup>3</sup> Li 20	<sup>4</sup> Be 0.03	<i>superconducting @ p &gt;&gt; 1 bar</i>																<sup>5</sup> B 11	<sup>6</sup> C	<sup>7</sup> N	<sup>8</sup> O 0.6	<sup>9</sup> F	<sup>10</sup> Ne
<sup>11</sup> Na	<sup>12</sup> Mg	<i>non-superconducting</i>																<sup>13</sup> Al 1.19	<sup>14</sup> Si 8.5	<sup>15</sup> P 18	<sup>16</sup> S 17	<sup>17</sup> Cl	<sup>18</sup> Ar
<sup>19</sup> K	<sup>20</sup> Ca 15	<sup>21</sup> Sc 0.35	<sup>22</sup> Ti 0.4	<sup>23</sup> V 5.3	<sup>24</sup> Cr	<sup>25</sup> Mn	<sup>26</sup> Fe 2.0	<sup>27</sup> Co	<sup>28</sup> Ni	<sup>29</sup> Cu	<sup>30</sup> Zn 0.9	<sup>31</sup> Ga 1.09	<sup>32</sup> Ge 5.4	<sup>33</sup> As 2.7	<sup>34</sup> Se 5.6	<sup>35</sup> Br 1.4	<sup>36</sup> Kr						
<sup>37</sup> Rb	<sup>38</sup> Sr 4.0	<sup>39</sup> Y 2.7	<sup>40</sup> Zr 0.55	<sup>41</sup> Nb 9.2	<sup>42</sup> Mo 0.923	<sup>43</sup> Tc 7.8	<sup>44</sup> Ru 0.5	<sup>45</sup> Rh 320 μK	<sup>46</sup> Pd	<sup>47</sup> Ag	<sup>48</sup> Cd 0.55	<sup>49</sup> In 3.4	<sup>50</sup> Sn 3.7	<sup>51</sup> Sb 5.6	<sup>52</sup> Te 7.4	<sup>53</sup> I 1.1	<sup>54</sup> Xe						
<sup>55</sup> Cs	<sup>56</sup> Ba 5.1	<sup>57</sup> La 5.9	<sup>72</sup> Hf 0.16	<sup>73</sup> Ta 4.4	<sup>74</sup> W 0.01	<sup>75</sup> Re 1.7	<sup>76</sup> Os 0.65	<sup>77</sup> Ir 0.14	<sup>78</sup> Pt	<sup>79</sup> Au	<sup>80</sup> Hg 4.15	<sup>81</sup> Tl 2.4	<sup>82</sup> Pb 7.2	<sup>83</sup> Bi 8.7	<sup>84</sup> Po	<sup>85</sup> At	<sup>86</sup> Pn						
<sup>87</sup> Fr	<sup>88</sup> Ra	<sup>89</sup> Ac	<sup>58</sup> Ce 1.7	<sup>59</sup> Pr	<sup>60</sup> Nd	<sup>61</sup> Pm	<sup>62</sup> Sm	<sup>63</sup> Eu	<sup>64</sup> Gd	<sup>65</sup> Tb	<sup>66</sup> Dy	<sup>67</sup> Ho	<sup>68</sup> Er	<sup>69</sup> Tm	<sup>70</sup> Yb	<sup>71</sup> Lu 0.1							
			<sup>90</sup> Th 1.37	<sup>91</sup> Pa 1.3	<sup>92</sup> U 0.2	<sup>93</sup> Np	<sup>94</sup> Pu	<sup>95</sup> Am 0.8	<sup>96</sup> Cm	<sup>97</sup> Bk	<sup>98</sup> Cf	<sup>99</sup> Es	<sup>100</sup> Fm	<sup>101</sup> Md	<sup>102</sup> No	<sup>103</sup> Lw							

elemental  
superconductors

# 1.6 Superconducting Materials

- *elemental superconductors*

- highest  $T_c$ : Nb, 9.2 K
- lowest  $T_c$ : Rh, 0.32 mK
- many elements become superconducting under pressure
  - e.g. Li:  $T_c$  almost 20 K @  $p = 0.5$  Mbar
  - non-magnetic high pressure Fe phase:  $T_c = 2$  K

- *problem related to observation of superconductivity in materials with very low  $T_c$ :*

$$k_B T_c = 1.38 \cdot 10^{-26} \text{ J} \quad @ \quad T_c = 1 \text{ mK}$$

requires small pair breaking rate  $\rightarrow$  very pure materials

$$\tau^{-1} \leq \frac{k_B T_c}{\hbar} = 1.38 \cdot 10^{-26} \frac{\text{J}}{\hbar} \quad @ \quad T_c = 1 \text{ mK} \Rightarrow \tau \geq 10^{-8} \text{ s}$$

# 1.6 Superconducting Materials

material	$T_c$
<i>@ 1 bar</i>	
Ru	0.35 K
Al	1.2 K
In	3.4 K
Sn	3.7 K
Hg, Ta	4.2 K
Pb	7.2 K
Nb	9.2 K
<i>@ &gt; 120 kbar</i>	
Si	6.7 K
Ge	5.4 K
S	17 K
Li	16 K

material	$T_c$
amorphous:	Pt 0.6 .. 0.9 K
quenched condensed:	Ga 8.0 K (orthorhombic phase: 1.09 K)
	Bi 6.0 K (crystalline phase: semimetal, no SC)



# 1.6 Superconducting Materials

- *alloys and intermetallic compounds*

- more than 1000 systems found until today
- some have high relevance for applications:

e.g. A15 compounds (1953) with with  $\beta$ -tungsten structure  
 $\text{Nb}_3\text{Ge}$ :  $T_c = 23.2$  K,  $\text{Nb}_3\text{Sn}$ :  $T_c = 18$  K,  $\text{V}_3\text{Si}$ :  $T_c = 17$  K

e.g.  $\text{NbTi}$ :  $T_c = 10 - 11$  K,  $\text{NbN}$ :  $T_c = 13 - 16$  K

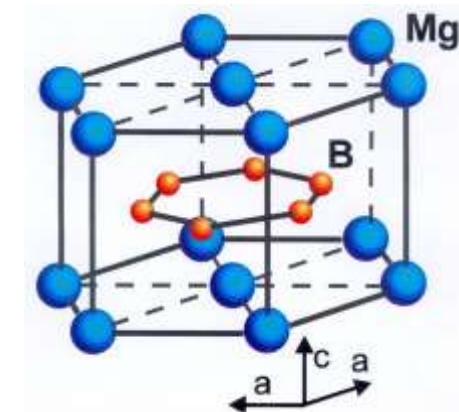
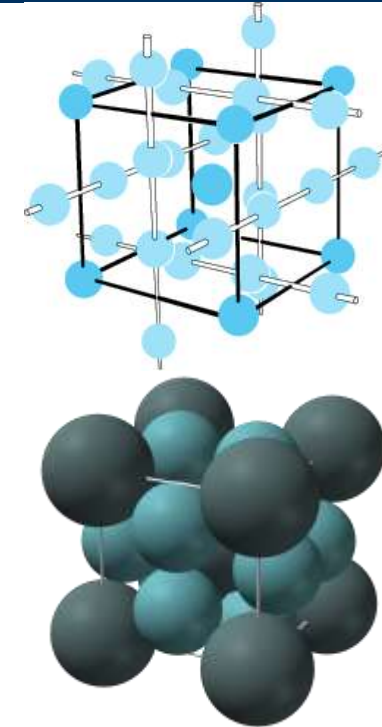
- Chevrel phases:  $M_x\text{Mo}_6\text{X}_8$   $M = \text{Ca, Sr, Ba, Sn, Pb, Au, RE}$   
 $X = \text{S, Se, Te}$  (chalcogenides)

e.g.  $\text{PbMo}_6\text{S}_8$ :  $T_c = 15$  K

- boron carbides:  $\text{RM}_2\text{B}_2\text{C}$   $R = \text{rare earth elem. (e.g. Tm, Er, Ho)}$   
 (1994)  $M = \text{Ni, Pd}$

e.g.  $(\text{Lu/Y})\text{Ni}_2\text{B}_2\text{C}$ :  $T_c = 16$  K

- $\text{MgB}_2$   $T_c$  almost 40 K  
 (2001)



# 1.6 Superconducting Materials

- *heavy Fermion superconductors*

- found by **Frank Steglich et al.** in 1979

- CeCu<sub>2</sub>Si<sub>2</sub>                       $T_c = 0.5$  K

- today many systems known

- electrons in these compounds have very large effective mass

- heavy Fermions:  $m^* \sim 100 - 1000 m_e$

- mechanism of superconductivity still under debate

# 1.6 Superconducting Materials

- *organic superconductors*

- found by **Jerome** et al. in 1980

- TMTSF (tetramethyl-tetraselenafulvalen)

$$T_c = 0.9 \text{ K}$$

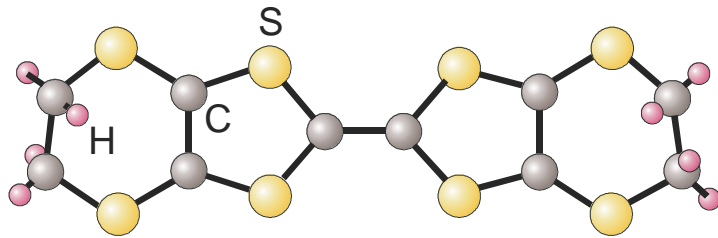
- today many systems known with  $T_c$  up to 12 K

e.g. (BEDT-TTF)<sub>2</sub>Cu[N(CN)<sub>2</sub>]Br

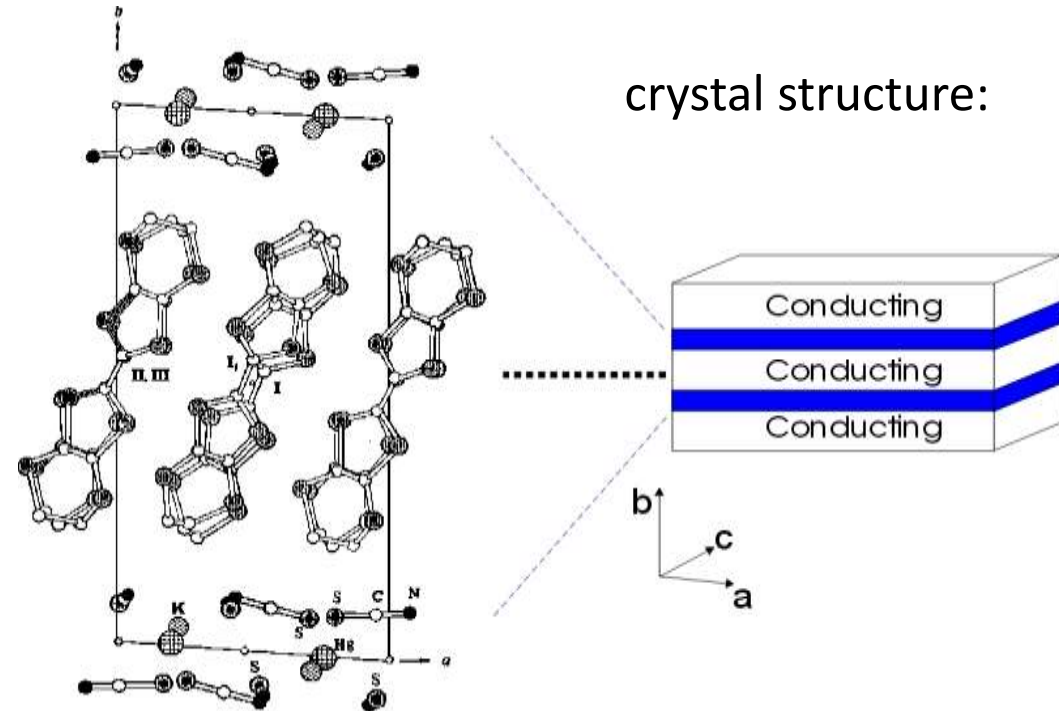
$$T_c = 11.2 \text{ K}$$

bis(ethylenedithio)-tetrathiafulvalene

BEDT-TTF-molecule:



- most systems are highly anisotropic



# 1.6 Superconducting Materials

- *fullerides*

- doping of  $C_{60}$  molecules (fullerene), arrangement in regular structure  $\rightarrow$  *fullerides*

- superconductivity found in 1991 by **Robert Haddon** at Bell Labs

$K_3C_{60}$  with  $T_c = 18$  K

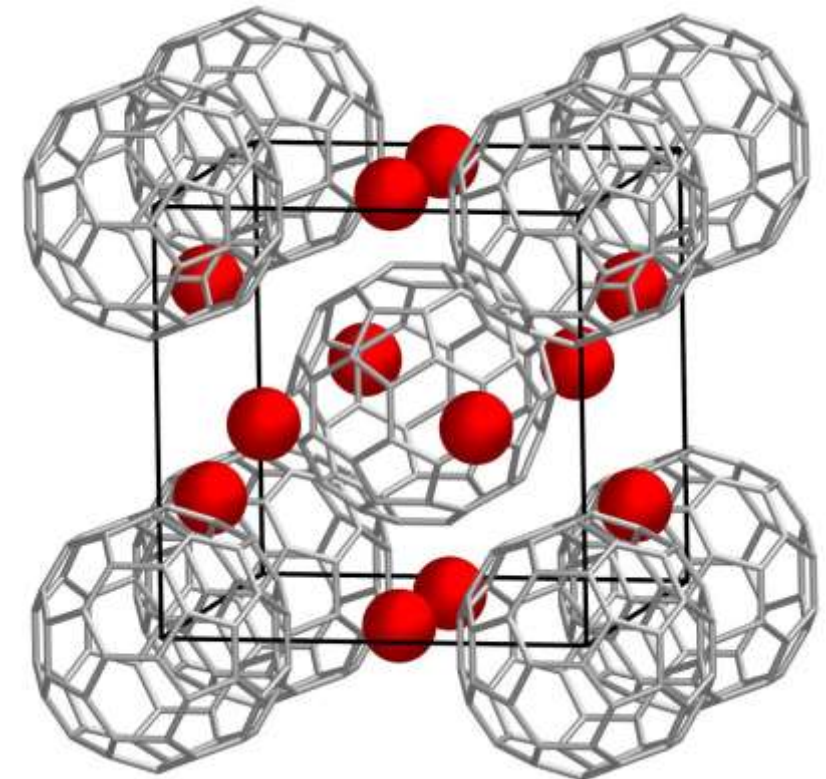
- until today  $T_c$  up to 40 K found

$Cs_2RbC_{60}$

$T_c = 33$  K

$Cs_3C_{60}$

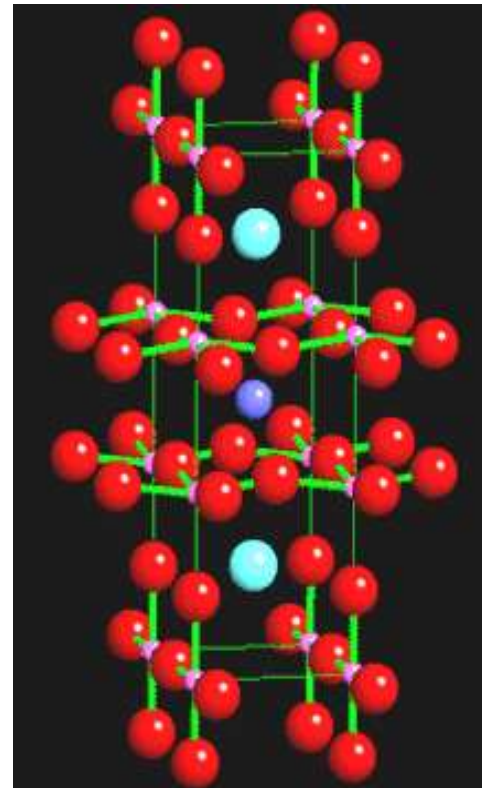
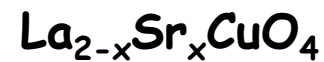
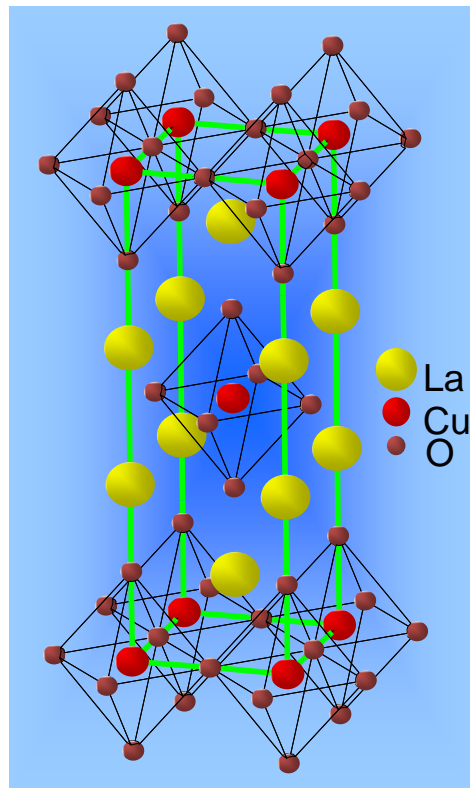
$T_c = 40$  K @  $p = 15$  kbar



# 1.6 Superconducting Materials

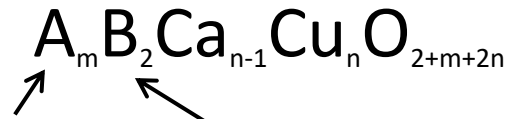
- *oxide superconductors*

- discovered by **Georg Bednorz** and **Alex Müller** in 1986 in  $\text{La}_{2-x}\text{Ba}_x\text{CuO}_4$  (Zurich oxide)
- until today several compounds found with  $T_c$  up to 135 K (165 K under pressure)
- layered crystal structure formed by  $\text{CuO}_2$  planes and charge reservoir layers



# 1.6 Superconducting Materials

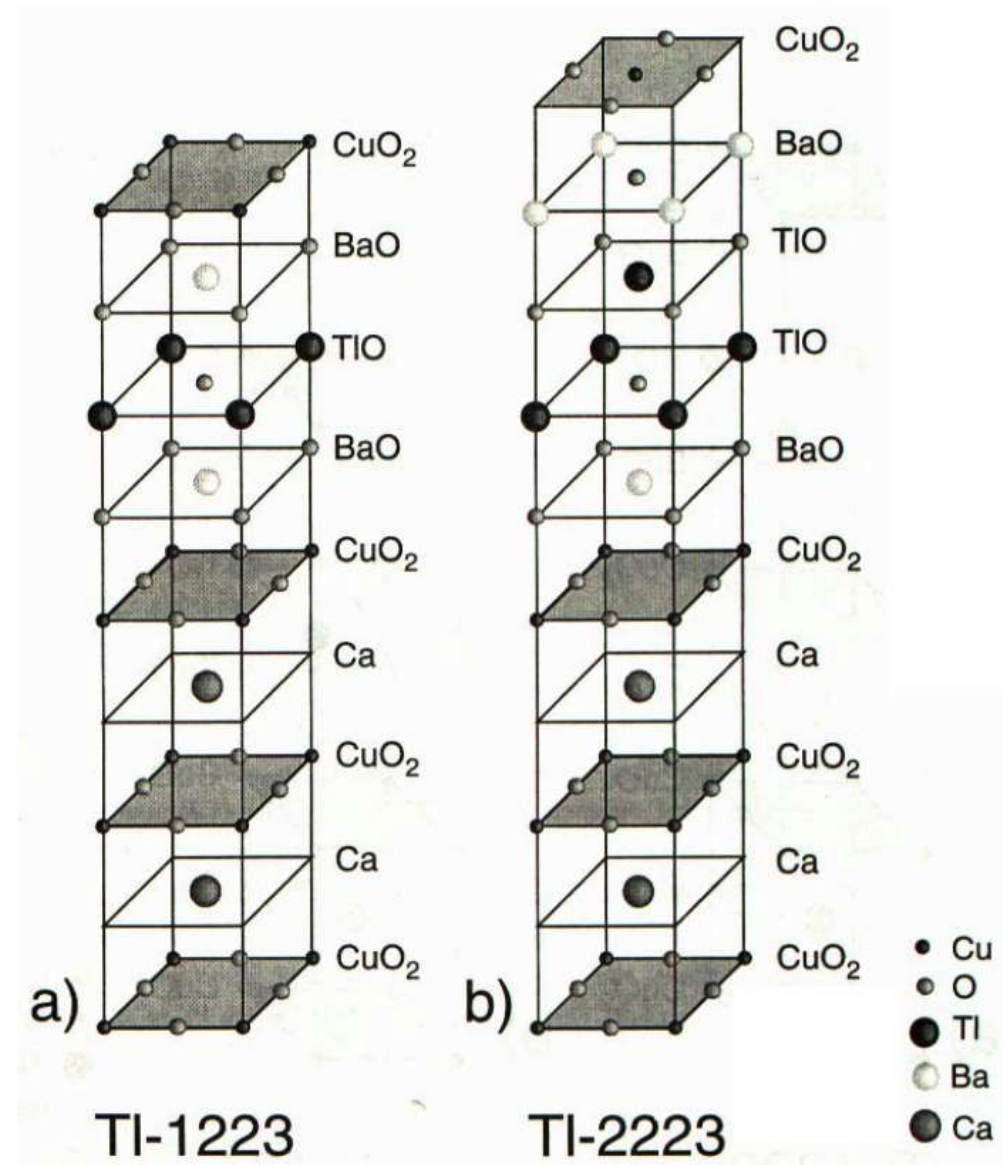
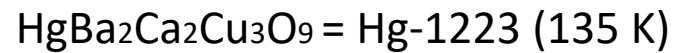
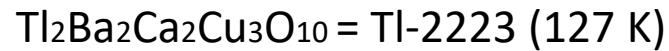
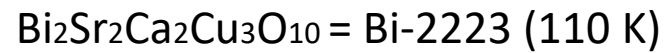
4 component systems



Bi, Tl, Hg

Ba, Sr = alkaline earth metals

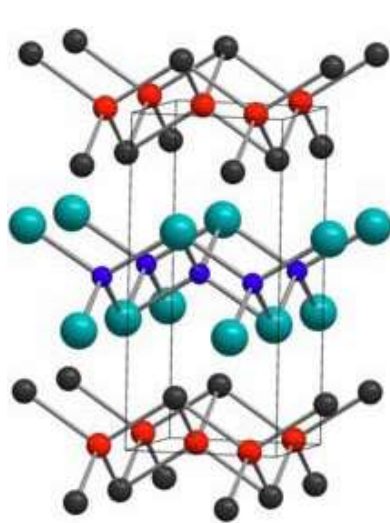
examples



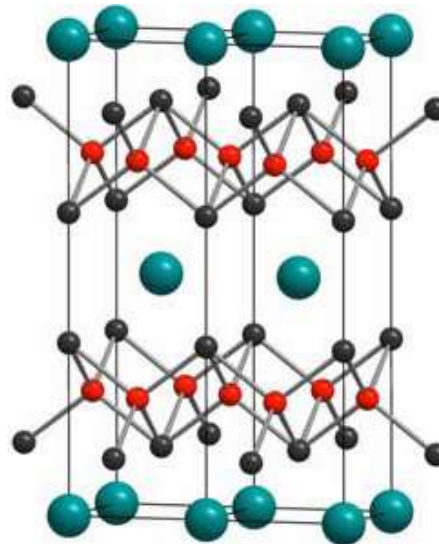
# 1.6 Superconducting Materials

- *iron pnictide superconductors*

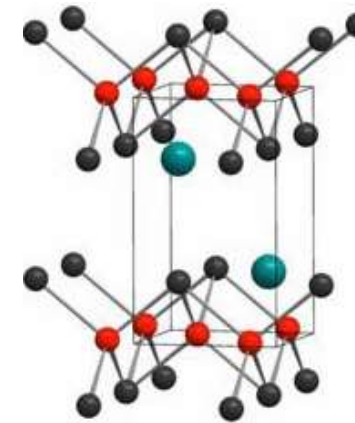
- discovered in 2006 by **Hideo Hosono** et al. in  $\text{La}[\text{O}_{1-x}\text{F}_x]\text{FeAs}$ ,  $T_c = 26$  K
- until today several compounds/families found with  $T_c$  up to 55 K



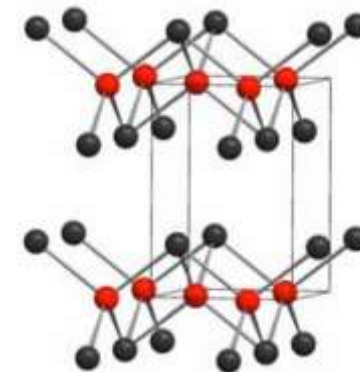
**LaFeAsO (1111)**



**BaFe<sub>2</sub>As<sub>2</sub> (122)**



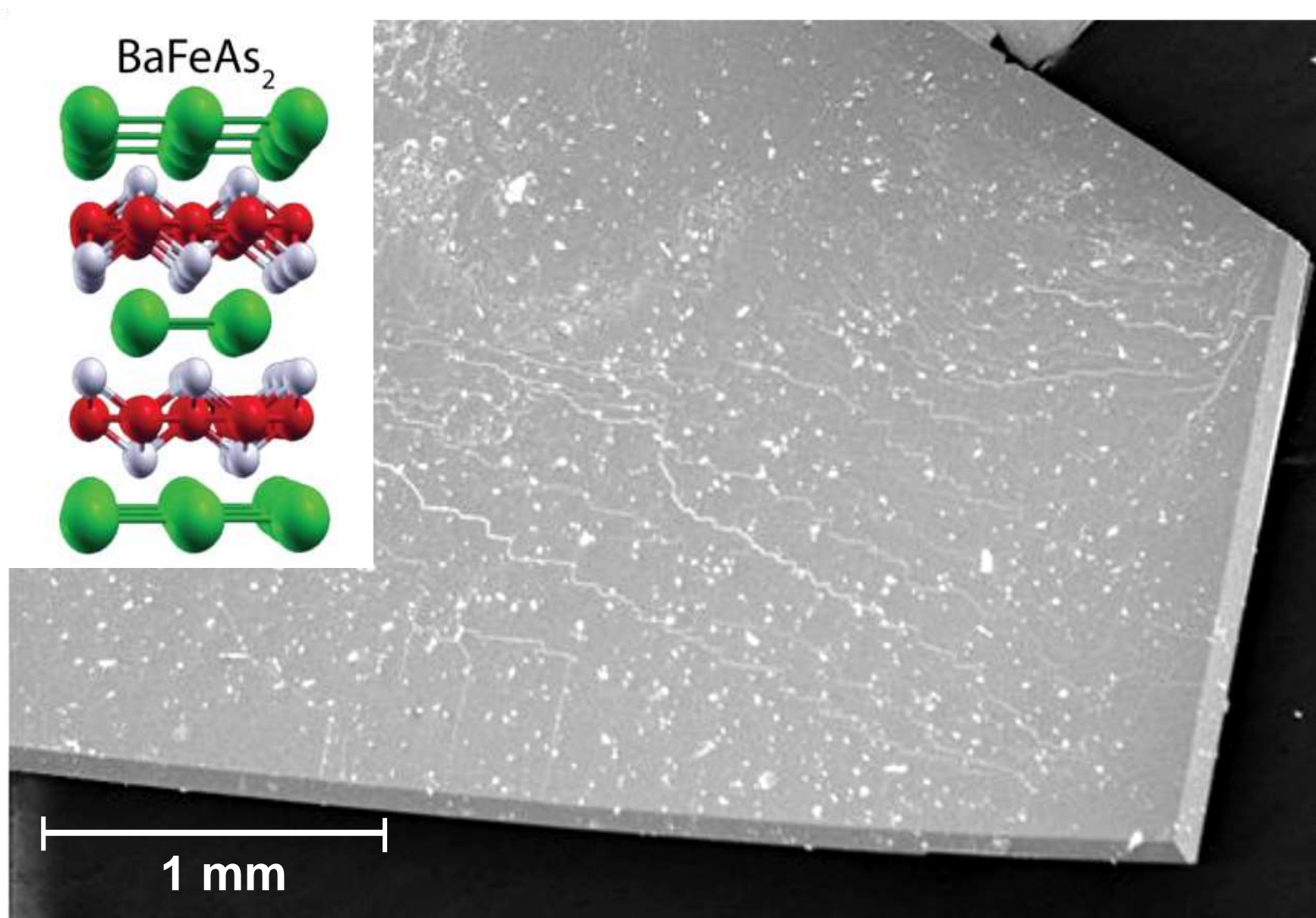
**LiFeAs (111)**



**FeSe (11)**

Yoichi Kamihara, Hidenori Hiramatsu, Masahiro Hirano, Ryuto Kawamura, Hiroshi Yanagi, Toshio Kamiya, and Hideo Hosono  
 "Iron-Based Layered Superconductor: LaOFeP". *J. Am. Chem. Soc.* **128** (31): 10012–10013 (2006).

# 1.6 Superconducting Materials





## **1. Basic Properties of Superconductors**

### **1.1 History of Superconductivity**

### **1.2 Perfect Conductivity**

### **1.3 Perfect Diamagnetism**

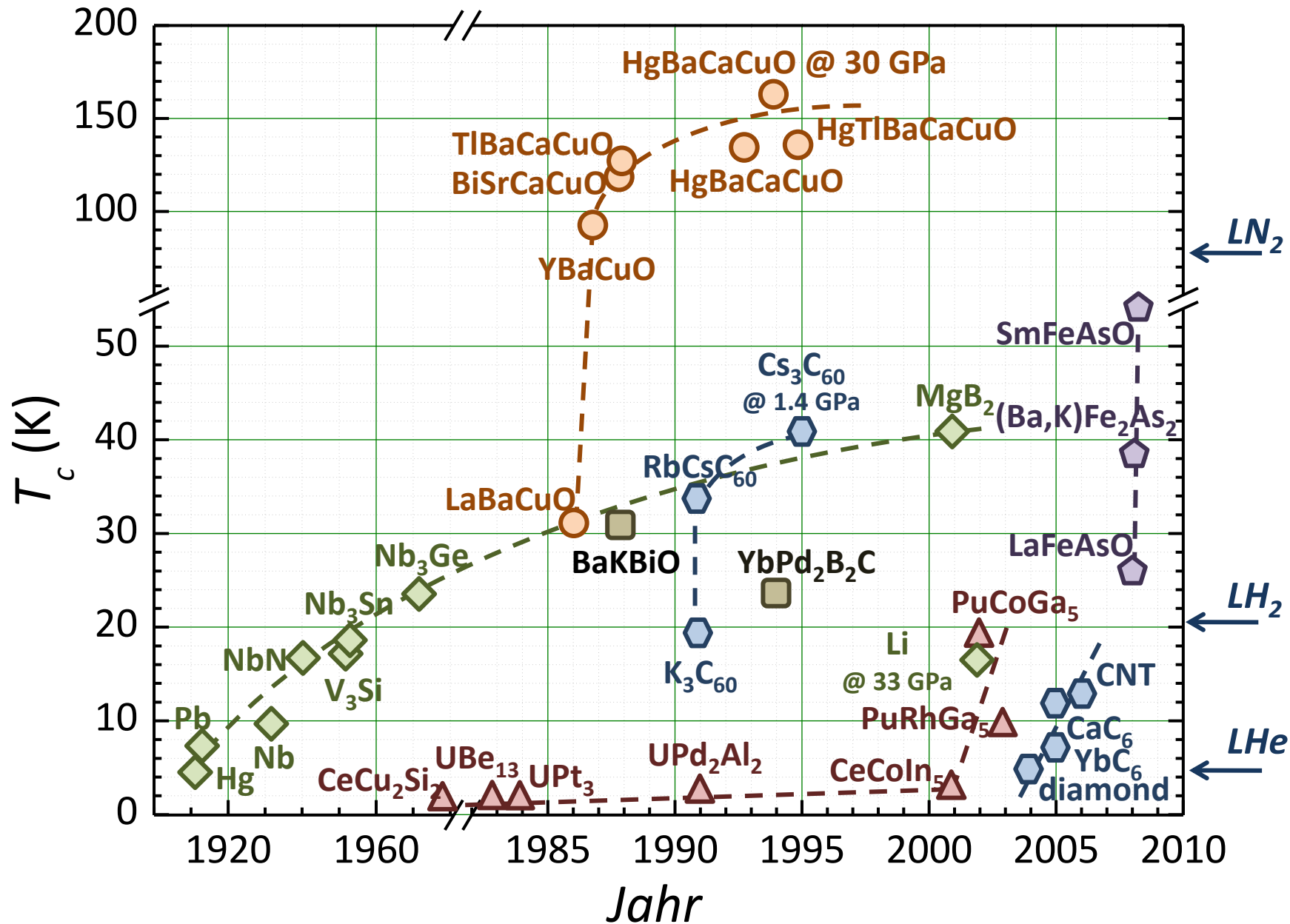
### **1.4 Type-I and Type-II Superconductors**

### **1.5 Flux Quantization**

### **1.6 Superconducting Materials**

### **1.7 Transition Temperatures**

# 1.7 Transition Temperatures



# 1.7 Transition Temperatures

- recently discovered materials with very high transition temperatures

- **2015:**

Eremets and co-workers report that H<sub>2</sub>S becomes a metallic conductor under high pressure (100–300 GPa) and shows a transition temperature of  $T_c = -70^\circ\text{C}$  (203 K).



LETTER

doi:10.1038/nature14964

Conventional superconductivity at 203 kelvin at high pressures in the sulfur hydride system

A. P. Drozdov<sup>1\*</sup>, M. I. Eremets<sup>1\*</sup>, I. A. Troyan<sup>1</sup>, V. Ksenofontov<sup>2</sup> & S. I. Shylin<sup>2</sup>

- **2019:**

Eremets *et al.* measured for LaH<sub>10</sub> under high pressure (170 GPa) a transition temperature of  $T_c \approx 250$  K ( $\approx -23^\circ\text{C}$ )

LETTER

https://doi.org/10.1038/s41586-019-1201-8

Superconductivity at 250 K in lanthanum hydride under high pressures

A. P. Drozdov<sup>1,7</sup>, P. P. Kong<sup>1,7</sup>, V. S. Minkov<sup>1,7</sup>, S. P. Besedin<sup>1,7</sup>, M. A. Kuzovnikov<sup>1,6,7</sup>, S. Mozaffari<sup>2</sup>, L. Balicas<sup>2</sup>, F. F. Balakirev<sup>3</sup>, D. E. Graf<sup>2</sup>, V. B. Prakapenka<sup>4</sup>, E. Greenberg<sup>4</sup>, D. A. Kryazev<sup>1</sup>, M. Tkacz<sup>5</sup> & M. I. Eremets<sup>1\*</sup>

# 1.7 Transition Temperatures

- recently discovered materials with very high transition temperatures

– 2020:

Snider *et al.* measured for  $\text{CH}_8\text{S}$  under high pressure (267 GPa) a transition temperature of  $T_c \approx 288 \text{ K}$  ( $\approx 15 \text{ }^\circ\text{C}$ ), Nature 586, 373 - 377 (2020)



## Article

### Room-temperature superconductivity in a carbonaceous sulfur hydride

<https://doi.org/10.1038/s41586-020-2801-z>

Received: 21 July 2020

Accepted: 8 September 2020

Published online: 14 October 2020

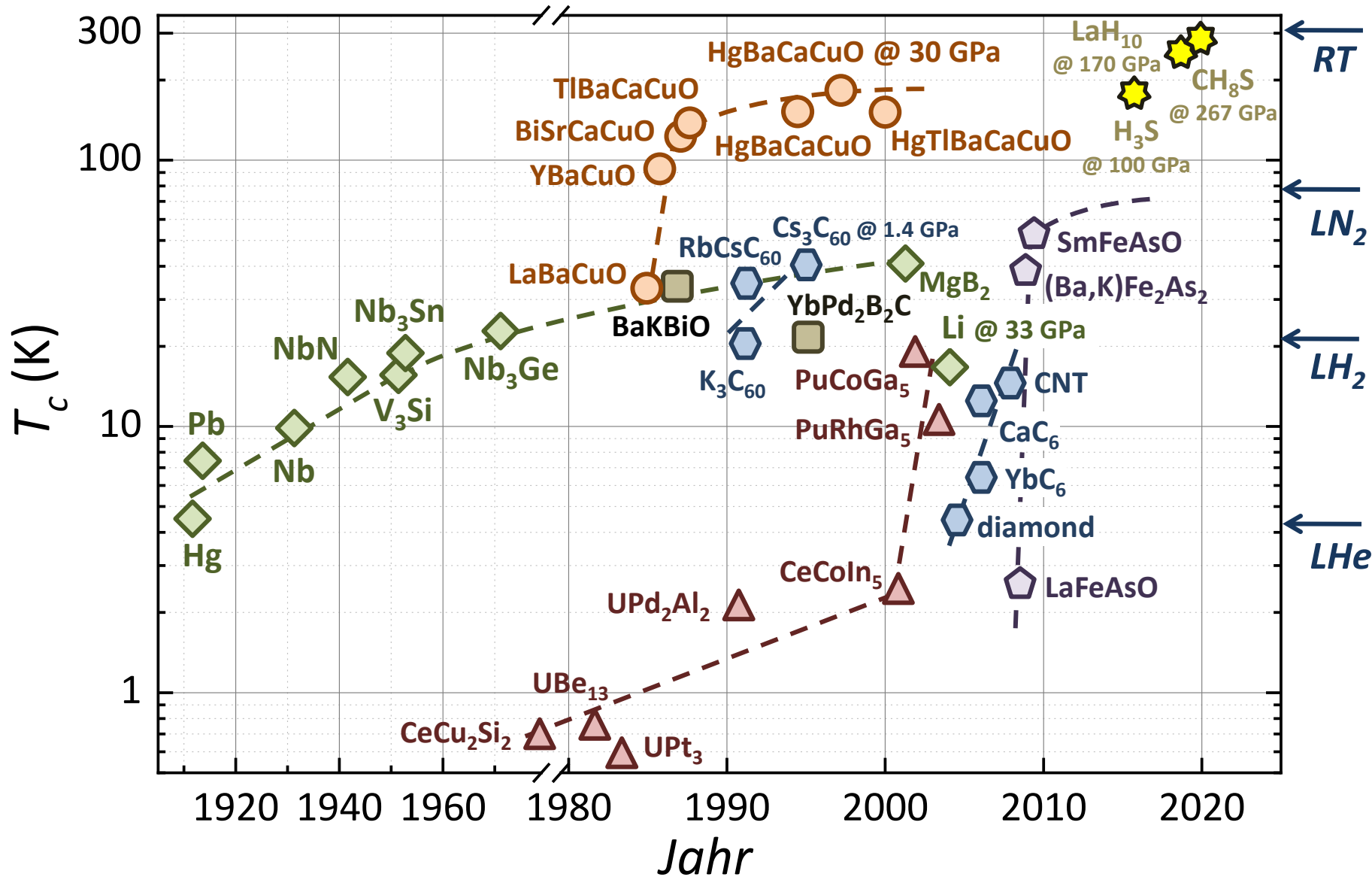
 Check for updates

Elliot Snider<sup>1,8</sup>, Nathan Dasenbrock-Gammon<sup>2,6</sup>, Raymond McBride<sup>1,8</sup>, Mathew Debessai<sup>3</sup>, Hiranya Vindana<sup>2</sup>, Kevin Vencatasamy<sup>2</sup>, Keith V. Lawler<sup>4</sup>, Ashkan Salamat<sup>5</sup> & Ranga P. Dias<sup>1,2,3,8</sup>

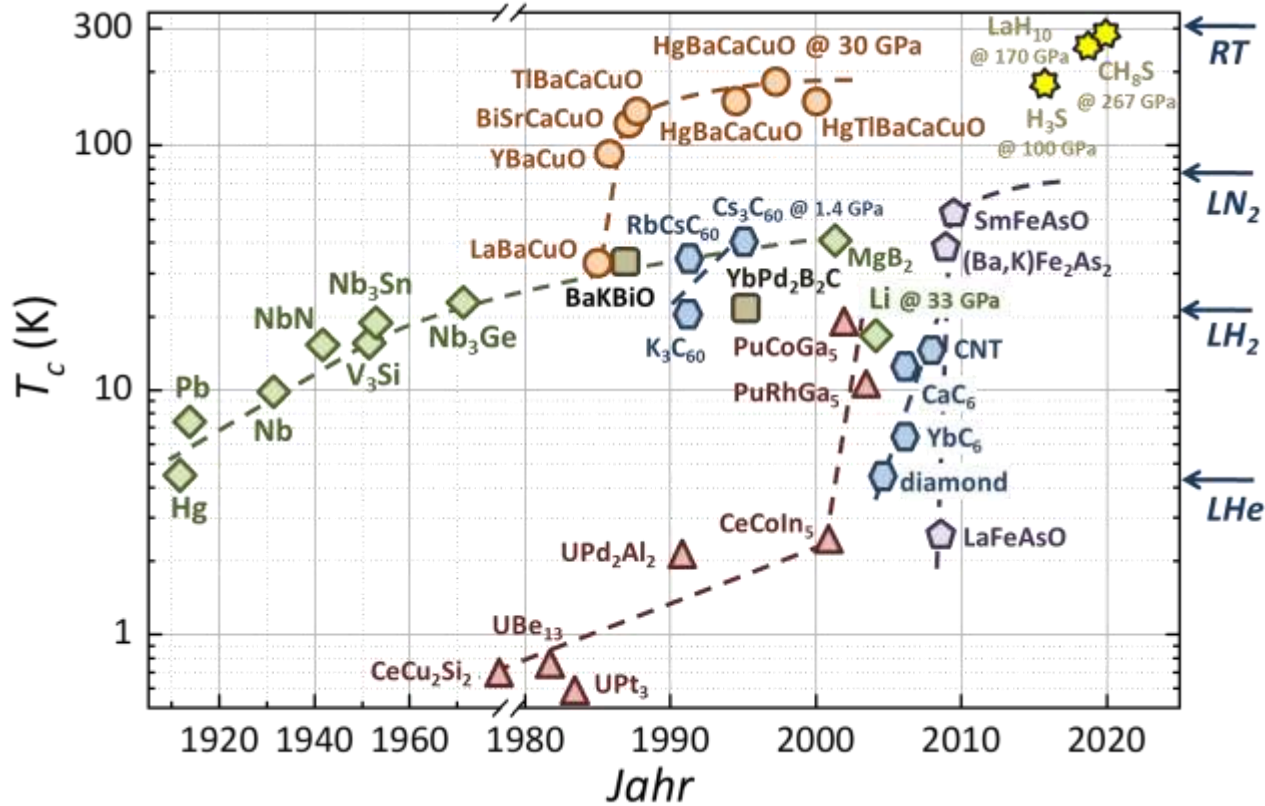
One of the long-standing challenges in experimental physics is the observation of room-temperature superconductivity<sup>1,2</sup>. Recently, high-temperature conventional superconductivity in hydrogen-rich materials has been reported in several systems under high pressure<sup>3-5</sup>. An important discovery leading to room-temperature superconductivity is the pressure-driven disproportionation of hydrogen sulfide

➔ material with the so far highest transition temperature

# 1.7 Transition Temperatures



# 1.7 Transition Temperatures



relevant material parameters for technical applications:

- high transition temperatures  $T_c$
- high critical current densities  $J_c$
- high critical magnetic fields  $B_c$

