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Meißner
Institut

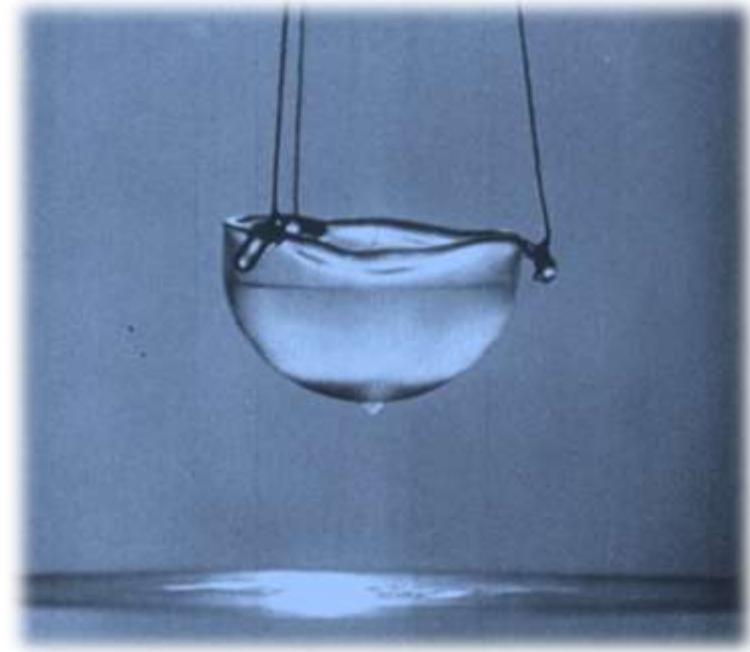


BAYERISCHE
AKADEMIE
DER
WISSENSCHAFTEN

Technische
Universität
München



Superconductivity and Low Temperature Physics II



Lecture Notes
Summer Semester 2024

R. Gross
© Walther-Meissner-Institut



*Superconductivity,
Superfluidity, Condensates, Quantum Liquids*

General Remarks on the Courses to the Field Superconductivity and Low Temperature Physics

1. Superconductivity and Low-Temperature Physics I + II

- Part I (WS 2023/2024): Foundations of Superconductivity
- Part II (SS 2024): Quantum Liquids, BECs, Quantum Interference Effects, Foundations of Low Temperature Physics and Techniques

This lecture

2. Applied Superconductivity I + II

-  → WS 2023/24 and SS 2024, 2 hrs lecture + 2 hrs exercises
- Josephson-Effect, Superconducting Electronics, Qubits, Quantum Circuits,

3. Seminars (SS 2024, WMI seminar room)

- Advances in Solid State Physics (TUE 10:15-11:45)
- Superconducting Quantum Circuits (TUE 12:15-13:45)



Further information: <https://www.wmi.badw.de/teaching>

- announcement of lectures
- downloads of lecture notes, handouts...
- seminar topics

Nobel Prizes in Physics related to LT Physics

year	name	discovery
1913	Heike Kamerlingh Onnes	"For his investigations on the properties of matter at low temperatures which led, inter alia, to the production of liquid helium "
1972	John Bardeen , Leon Neil Cooper and Robert Schrieffer	"for their jointly developed theory of superconductivity , usually called the BCS-theory "
1973	Brian David Josephson	"for his theoretical predictions of the properties of a supercurrent through a tunnel barrier, in particular those phenomena which are generally known as the Josephson effect "
1978	Pjotr Kapiza	"for his basic inventions and discoveries in the area of low-temperature physics"
1985	Klaus von Klitzing	"for the discovery of the quantized Hall effect "
1987	Johannes Georg Bednorz und Karl Alex Müller	"for their important break-through in the discovery of superconductivity in ceramic materials"
1996	David M. Lee , Douglas D. Osheroff und Robert C. Richardson	"for their discovery of superfluidity in helium-3 "
1997	Steven Chu , Claude Cohen-Tannoudji and William D. Phillips	"for development of methods to cool and trap atoms with laser light" See Laser cooling .
1998	Robert B. Laughlin , Horst Ludwig Störmer and Daniel Chee Tsui	"for their discovery of a new form of quantum fluid with fractionally charged excitations". See Quantum Hall effect .
2001	Eric A. Cornell , Wolfgang Ketterle and Carl E. Wieman	"for the achievement of Bose-Einstein condensation in dilute gases of alkali atoms, and for early fundamental studies of the properties of the condensates"
2003	Alexei Abrikosov , Witali Ginsburg and Anthony James Leggett	"for pioneering contributions to the theory of superconductors and superfluids"
2016	David J. Thouless , F. Duncan M. Haldane , J. Michael Kosterlitz	"for theoretical discoveries of topological phase transitions and topological phases of matter"

Contents of Lecture

Superconductivity and Low Temperature Physics I

Introduction

1. Basic Properties of Superconductors
2. Phenomenological Models of Superconductivity :
 - London equations
 - macroscopic quantum model
 - Ginzburg-Landau theory
3. Thermodynamics
4. Microscopic (BCS) theory
5. Flux pinning and critical currents
6. High Temperature Superconductivity
7. Applications

Superconductivity and Low Temperature Physics II

1. Quantum Gases & Liquids: Bose-Einstein condensation, Superfluid Helium (^4He and ^3He)
2. Quantum Interference Effects in Mesoscopic Conductors
3. Low Temperature Techniques
(generation and measurement of low temperatures)

Contents Part I: Quantum Liquids

I.1 Foundations and General Properties

- I.1.1 Quantum Gases & Liquids
- I.1.2 Helium
- I.1.3 Van der Waals Bonding
- I.1.4 Zero-Point Fluctuations
- I.1.5 Helium under Pressure
- I.1.6 pT-Phase Diagram of ^4He and ^3He
- I.1.7 Characteristic Properties of ^4He and ^3He
- I.1.8 Specific Heat of ^4He and ^3He

I.2 ^4He as an Ideal Bose Gas

- I.2.1 Bose-Einstein Condensation
- I.2.2 Ideal Bose Gas
- I.2.3 Bose Gas with Interactions
- I.2.4 Bose-Einstein Condensation of ^4He

I.3 Superfluid ^4He

- I.3.1 Two-Fluid Model
- I.3.2 Experimental Observations
- I.3.3 Two-Fluid Hydrodynamics
- I.3.4 Excitation Spectrum of ^4He

I.4 Vortices

- I.4.1 Quantization of Circulation
- I.4.2 Experimental Study of Vortices

I.5 ^3He

- I.5.1 normal fluid ^3He
- I.5.2 solid ^3He and Pomeranchuk effect
- I.5.3 superfluid ^3He

I.6 $^3\text{He} / ^4\text{He}$ mixtures

Contents Part II: Quantum Transport in Nanostructures

II.1 Introduction

- II.1.1 General Remarks
- II.1.2 Mesoscopic Systems
- II.1.3 Characteristic Length Scales
- II.1.4 Characteristic Energy Scales
- II.1.5 Transport Regimes

II.4 From Quantum Mechanics to Ohm's Law

II.5 Coulomb Blockade

II.2 Description of Electron Transport by Scattering of Waves

- II.2.1 Electron Waves and Waveguides
- II.2.2 Landauer Formalism
- II.2.3 Multi-terminal Conductors
- II.2.4 Statistics of Charge Transport

II.3 Quantum Interference Effects

- II.3.1 Double Slit Experiment
- II.3.2 Two Barriers – Resonant Tunneling
- II.3.3 Aharonov-Bohm Effect
- II.3.4 Weak Localization
- II.3.5 Universal Conductance Fluctuations

III.1 Generation of Low Temperatures

- III.1.1 Introduction
- III.1.2 Expansion Machine
- III.3 Regenerative Machine
- III.1.4 Joule-Thomson Cooling
- III.1.5 Summary
- III.1.6 Evaporation Cooling
- III.1.7 Dilution Cooling
- III.1.8 Pomeranchuk Cooling
- III.1.9 Adiabatic Demagnetization

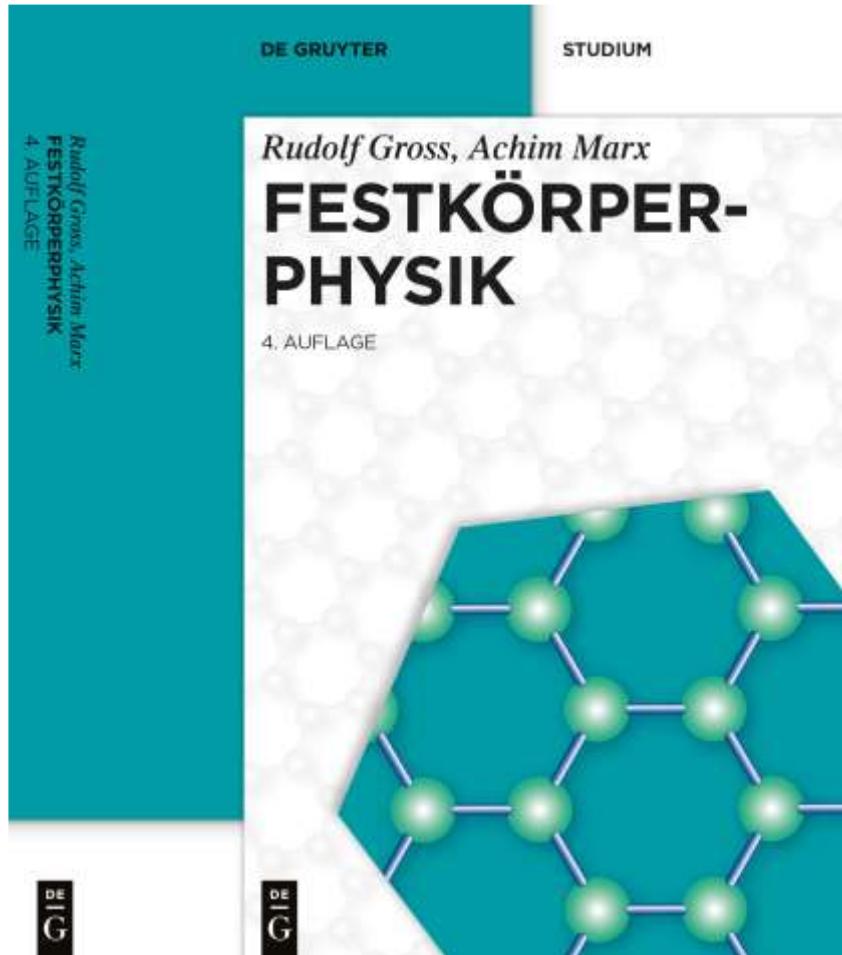
III.2 Thermometry

- III.2.1 Introduction
- III.2.2 Primary Thermometers
- III.2.3 Secondary Thermometers

Literature

- F. Pobell
Matter and Methods at Low Temperatures, Springer 1996
- D.R. Tilley and J. Tilley
Superfluidity and Superconductivity, Adam Hilger 1990
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Quantum Liquids - Bose Condensation and Cooper Pairing in Condensed-Matter Systems, Oxford University Press, 2022
- J. Wilks, D.S. Betts
Introduction to Liquid Helium, Oxford 1987
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Experimental Techniques in Low Temperature Physics, Oxford University Press, 2002
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- H. Frey, R.A. Haefer
Tieftemperaturtechnologie, VDI-Verlag, Düsseldorf 1981
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Introduction to Mesoscopic Physics, Oxford University Press, Oxford (1997)
- Supriyoto Datta
Electronic Transport in Mesoscopic Systems, Cambridge University Press, Cambridge (1995)
- Thomas Heinzel
Mesoscopic Electronic in Solid State Nanostructures, Wiley VCH, Weinheim (2003)
- Thomas Ihn
Semiconductor Nanostructures, Oxford University Press (2010)

Literature



Rudolf Gross, Achim Marx

Title: Festkörperphysik, 4th revised and extended edition

Publisher: Walter de Gruyter GmbH, Berlin/Boston

Published: January 2023

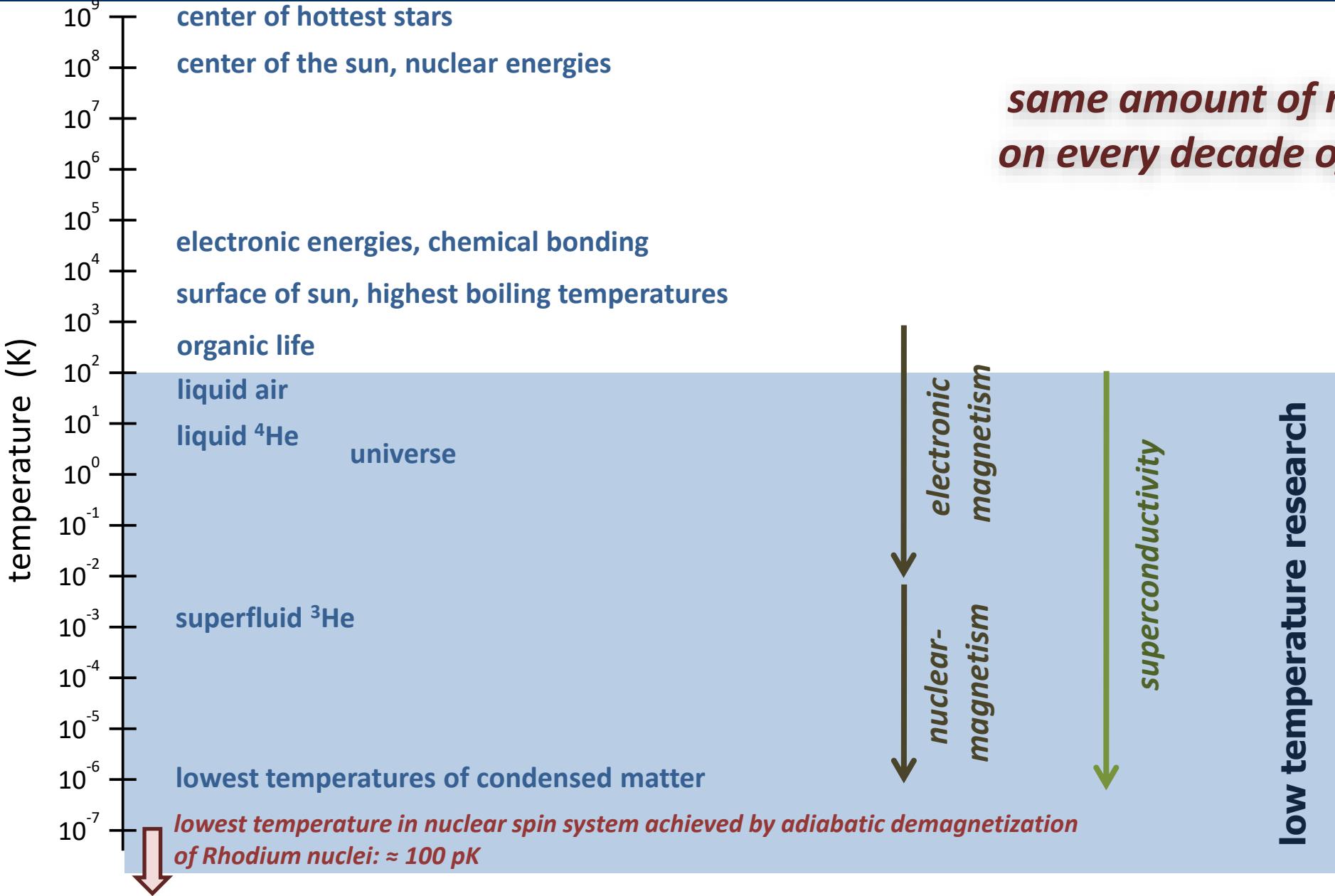
Language: German

9783110782349 (hardcover), ISBN 9783110782394 (eBook)

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Introduction

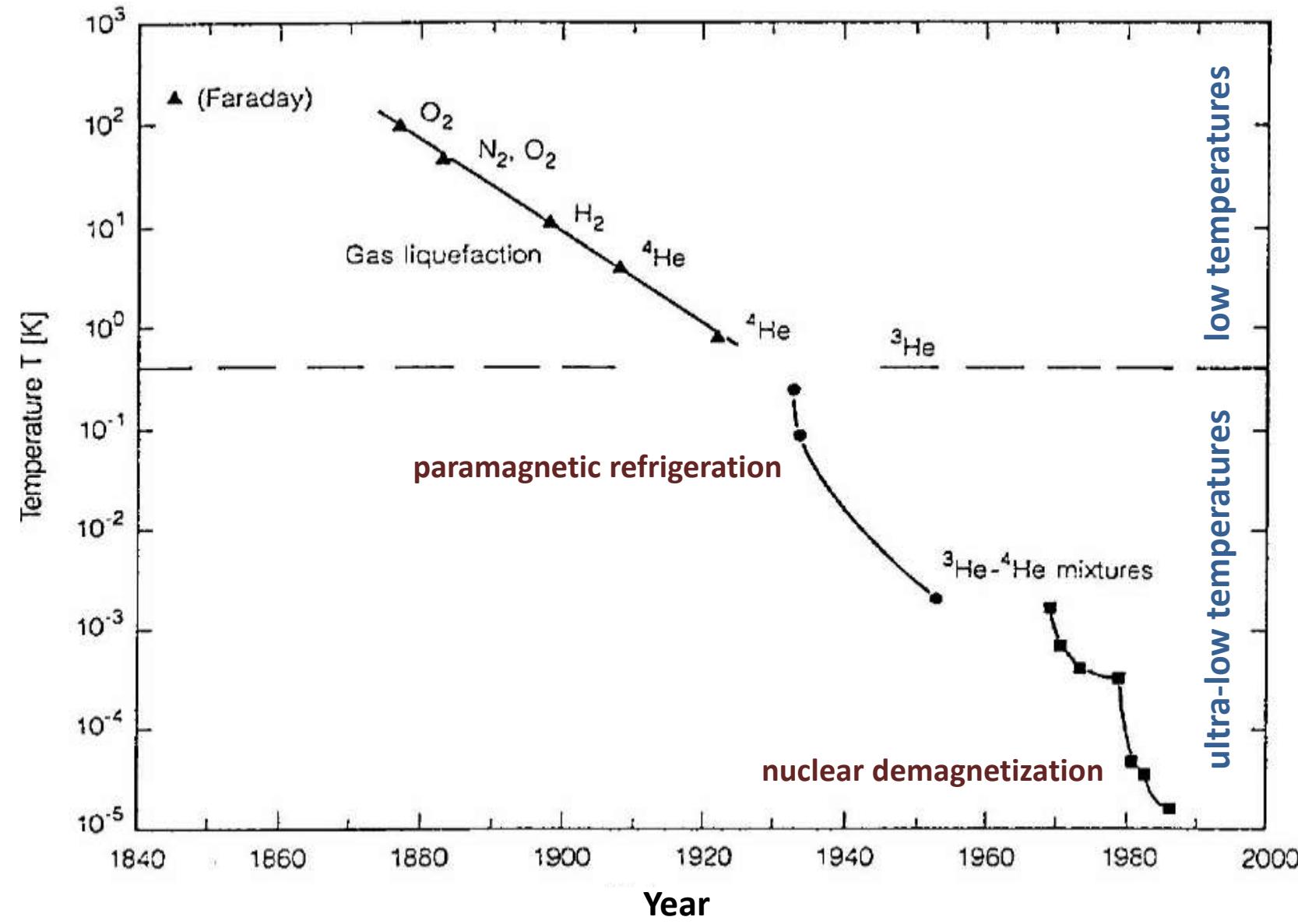
Temperature Scale



Low Temperature Phenomena

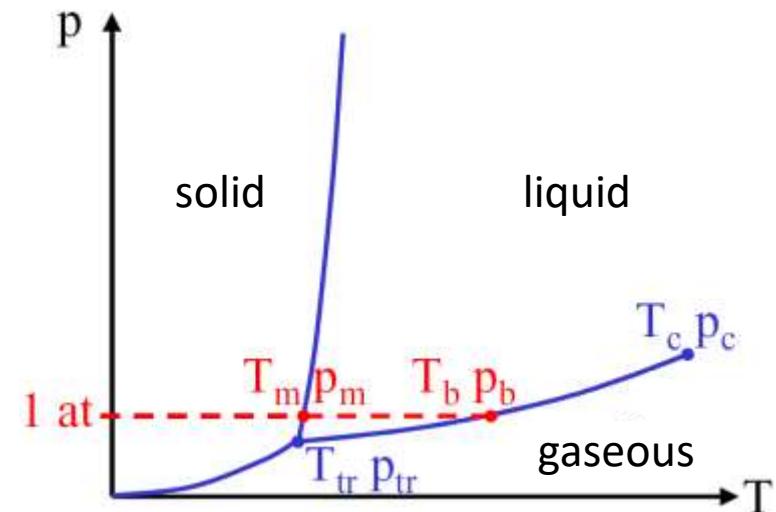
- many direct implications of quantum mechanics only show up at sufficiently low temperatures
 - e.g. magnetism, superconductivity
 - particularly interesting are quantum phenomena manifesting themselves on a macroscopic length scale
→ *macroscopic quantum phenomena*
 - Superconductivity
 - **Superfluidity**
 - **Bose-Einstein Condensation**
- } this lecture

Generation of Low Temperatures



Generation of Low Temperatures

Substance	T_b [K]	T_m [K]	T_{tr} [K]	P_{tr} [bar]	T_c [K]	P_c [bar]
$\underbrace{\quad\quad\quad}_{@ 1 \text{ bar}}$						
H_2O	373.15	273.15	273.16	0.06	647.3	220
Xe	165.1	161.3	161.4	0.82	289.8	58.9
Kr	119.9	115.8	114.9	0.73	209.4	54.9
O_2	90.2	54.4	54.36	0.016	154.3	50.4
Ar	87.3	83.8	83.81	0.67	150.9	48.7
N_2	77.4	63.3	63.15	0.12	126.0	33.9
Ne	27.1	24.5	24.56	0.43	44.5	27.2
D_2	23.7	18.7	18.72	0.17	38.3	16.6
H_2	20.3	14.0	13.80	0.07	33.3	13.0
4He	4.21	--	--	--	5.20	2.28
3He	3.19	--	--	--	3.32	1.16



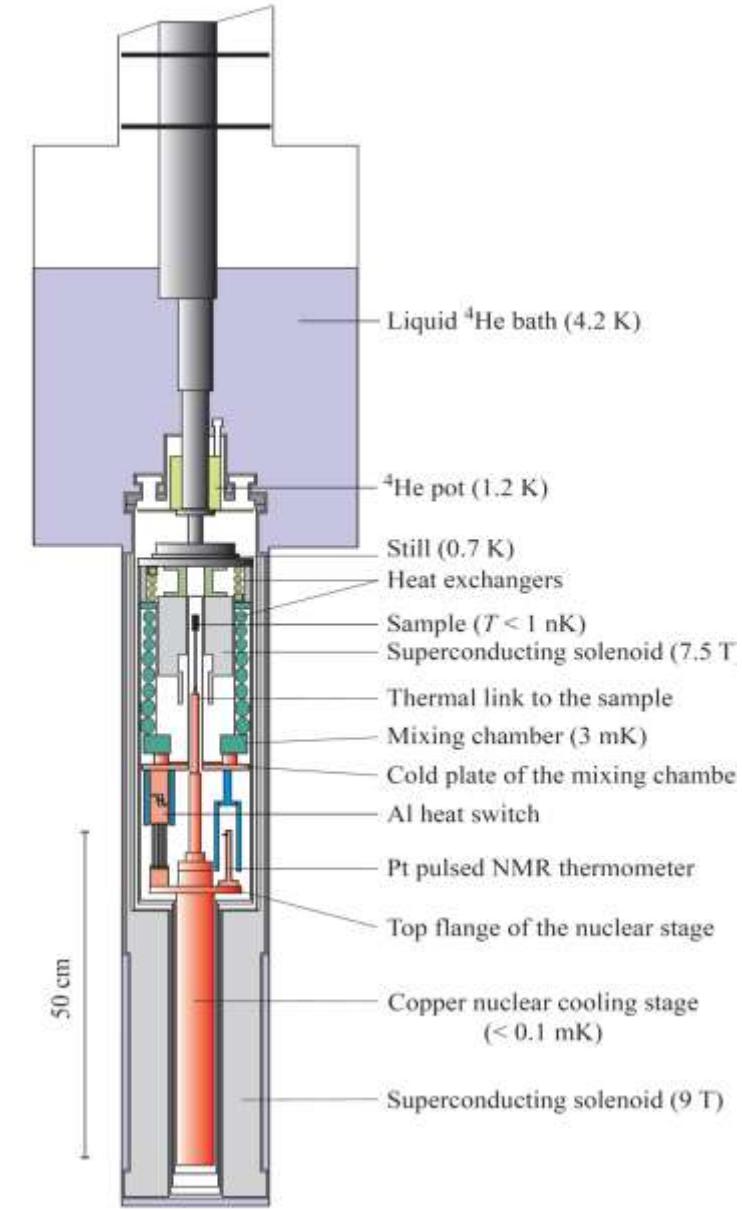
Generation of Low Temperatures

- nuclear demagnetization

experimental setup according to
Tauno Knuuttila (2000)

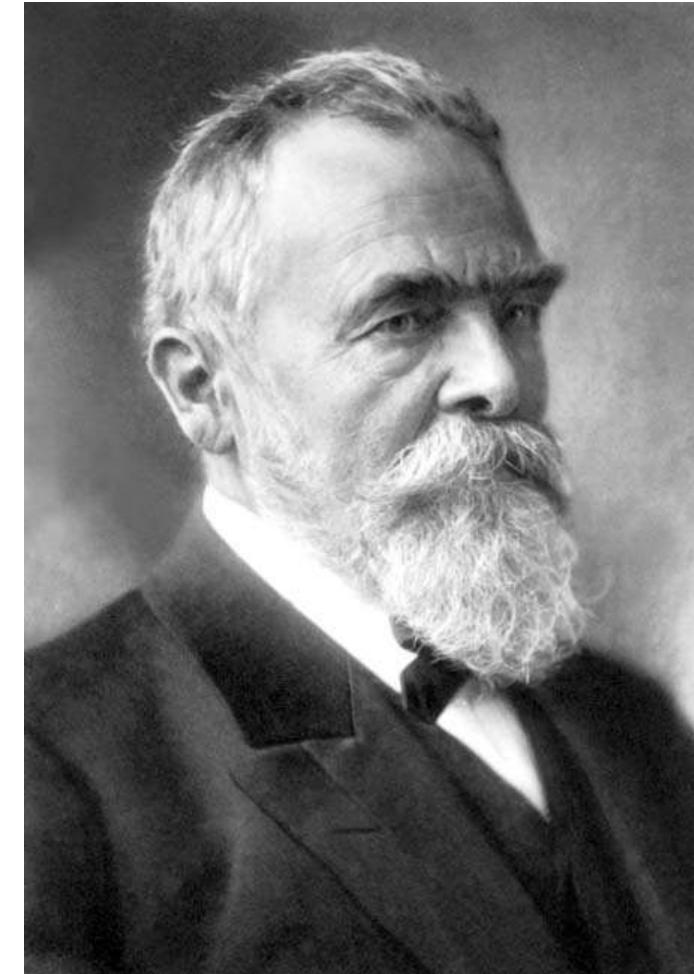
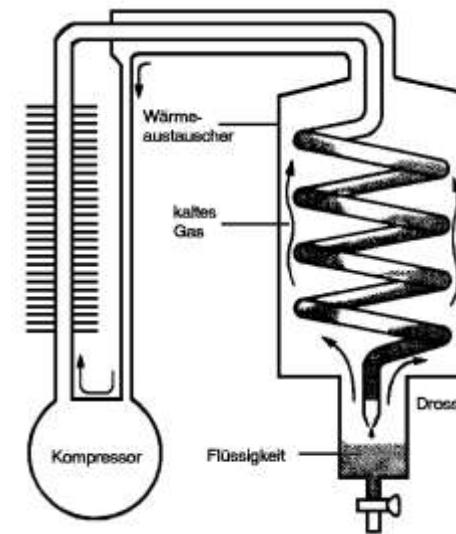
lowest temperature of nuclear spin system:
about **100 pK**
by demagnetization of Rhodium nuclei

PhD Thesis,
Helsinki University of Technology
(Espoo, Finland)



Low Temperature Technology

- 1868** offer of chair at the Polytechnische Schule München (now TUM)
- 1873** development of cooling machine allowing the temperature stabilization in beer brewing
- 21. 6. 1879** foundation of „*Gesellschaft für Linde's Eismaschinen AG*“ together with two beer brewers and three other co-founders
- 1892 – 1910** re-establishment of professorship
- 12.5.1903** patent application:
„*Lindesches Gegenstrom-verfahren*“
liquefaction of oxygen
($-182^{\circ}\text{C} = 90\text{ K}$)



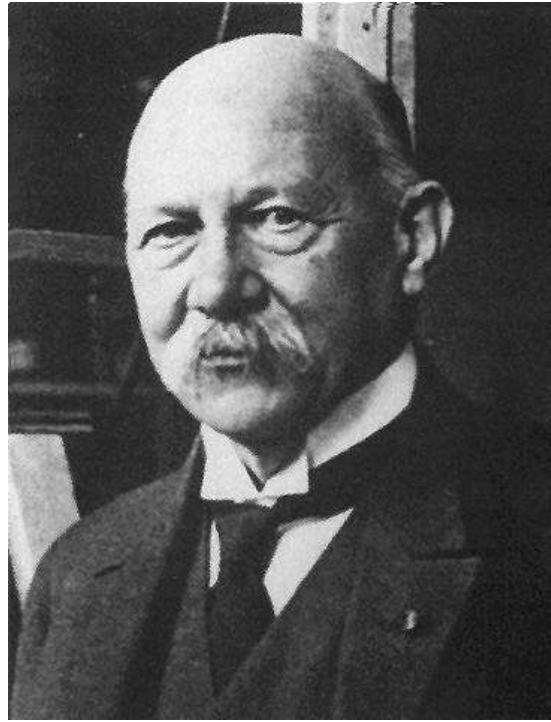
Carl Paul Gottfried von Linde
* 11. Juni 1842 in Berndorf, Oberfranken
† 16. November 1934 in Munich

Low Temperature Technology

- 1930** Linde AG uses the first cooling turbines for the generation of low temperatures
turbines have higher efficiency and therefore are used today in all larger liquefaction machines
e.g. He liquefier at the Walther-Meißner-Institut
- 1947** first commercial He liquefier (design by engineer Collins, therefore denoted as „Collins“ machine)
Arthur D. Little Inc. (today CTI)
- 1966** *Hall* et al. and *Neganov* et al. develop $^3\text{He}/^4\text{He}$ dilution refrigerators, generation of temperatures down to 2 mK

Discovery of Superconductivity (1911)

Heike Kamerlingh Onnes (1853-1926)

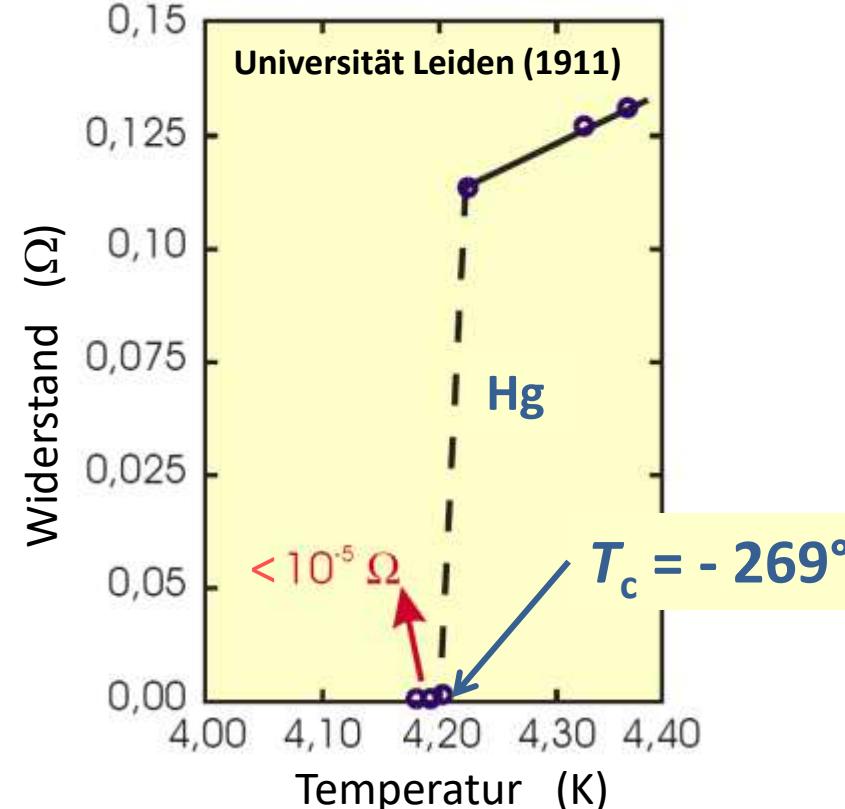


- Helium liquefaction: 1908
- discovery of superconductivity: 1911

Nobel Price in Physics 1913

choice of name:

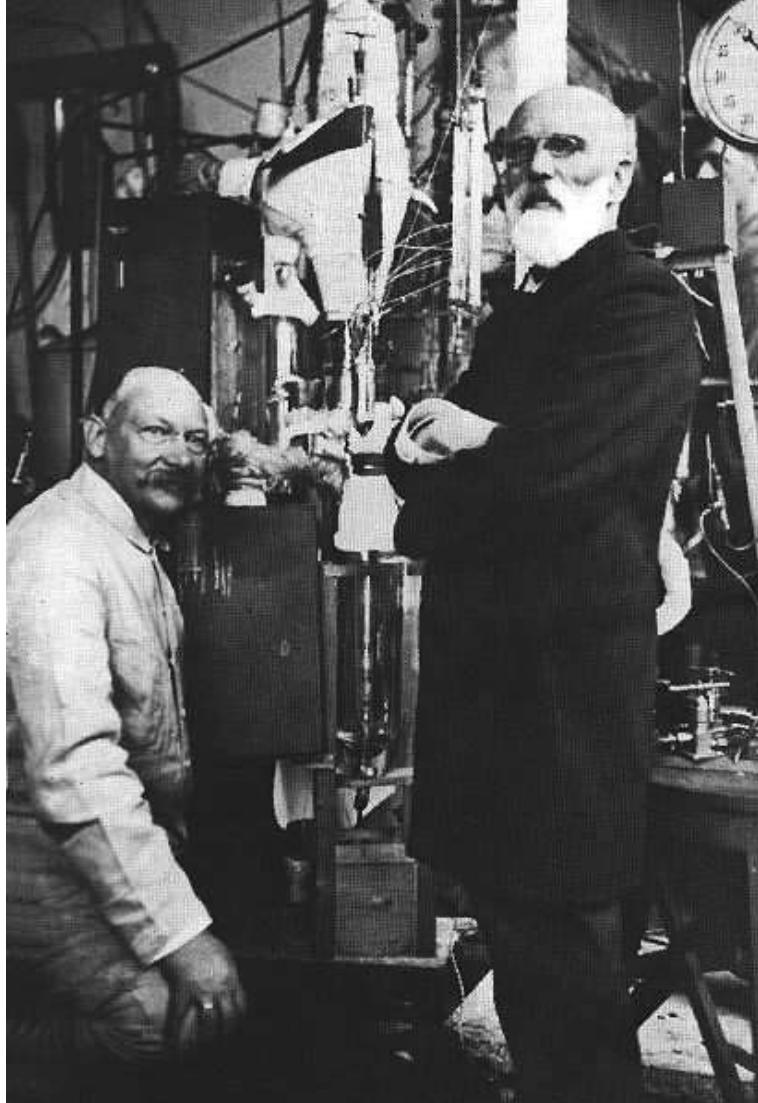
infinite electrical conductivity → **superconductivity**



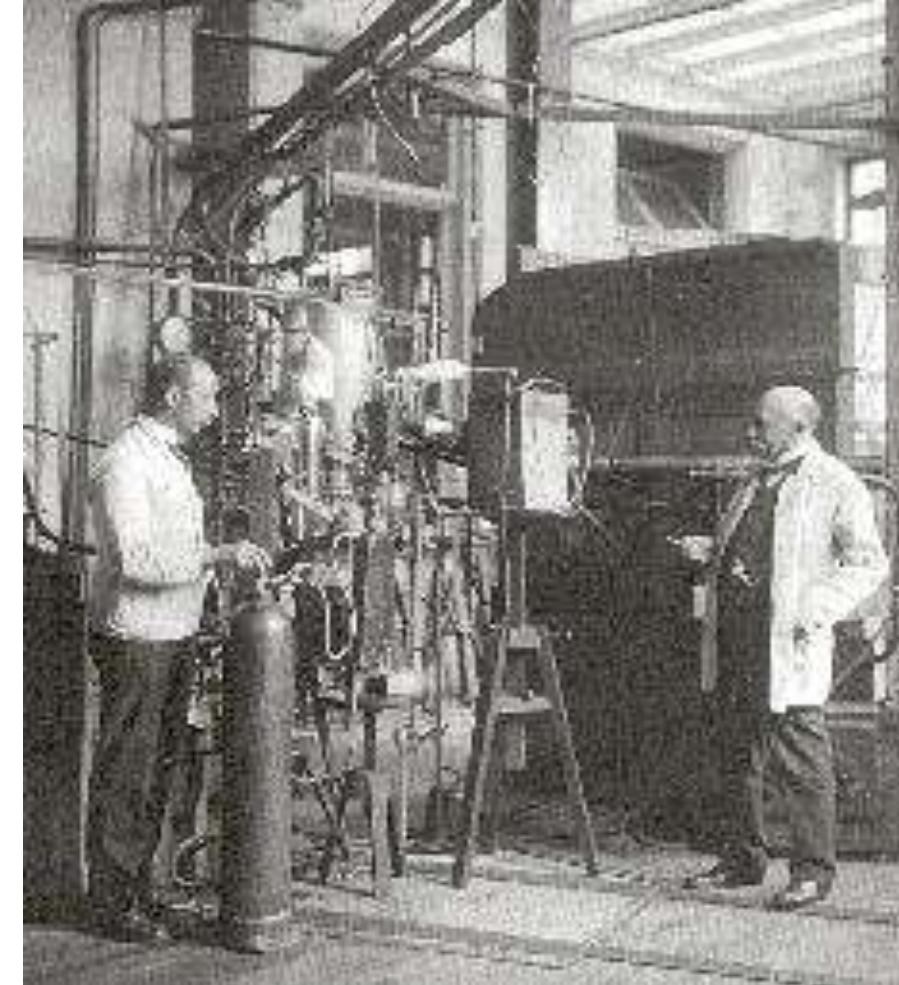
H. K. Onnes, Comm. Leiden 120b (1911)

*"for his investigations on the properties of matter at low temperatures which led, *inter alia* to the production of liquid helium"*

Discovery of Superconductivity (1911)



Kamerlingh Onnes and van der Waals



Kamerlingh Onnes and Technician Flim

Discovery of the Meißner-Ochsenfeld Effect (1933)



**Robert Ochsenfeld
(1901 – 1993)**



perfect diamagnetism



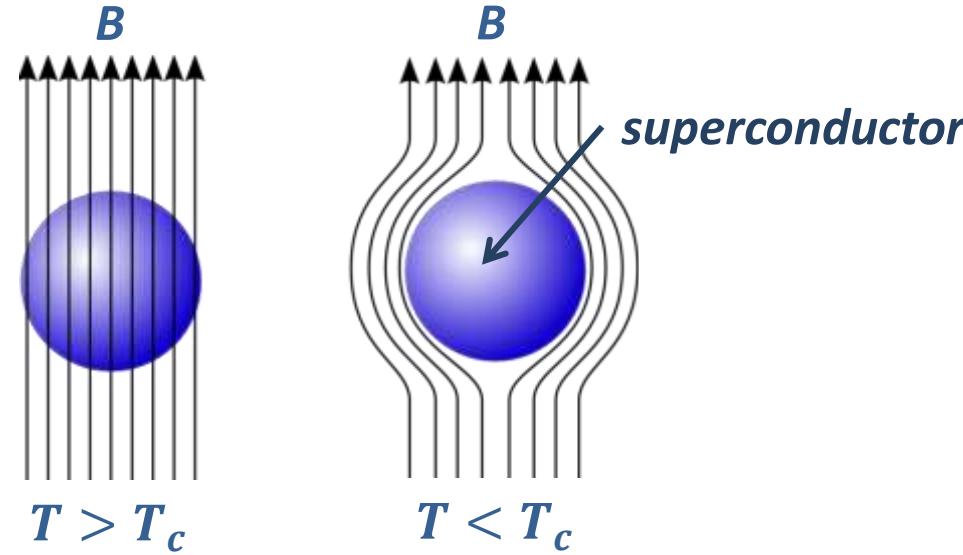
Dr. Walther Meissner
a. Prof. für technische Physik, Präsident 1946–50

**Walther Meißner
(1882 – 1974)**

*W. Meißner, R. Ochsenfeld,
Ein neuer Effekt bei Eintritt der Supraleitfähigkeit,
Naturwissenschaften 21, 787 (1933).*

Discovery of the Meißner-Ochsenfeld Effect (1933)

Walther Meißner (1882 – 1974)



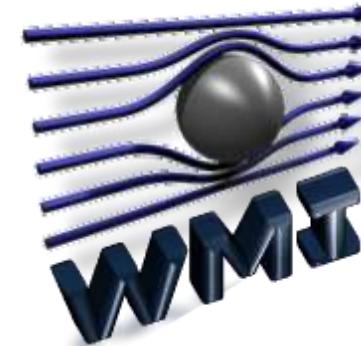
superconductors perfectly expel magnetic field

$$B_{\text{in}} = (1 + \chi) B_{\text{ext}} = 0 \quad \chi = \text{magnetic susceptibility}$$

ideal diamagnetism, $\chi = -1$

choice of name for perfect diamagnetism:

Meißner-Ochsenfeld Effect



Walther Meißner (1882 – 1974)

1913 – 1934 building and heading of low temperature laboratory at the Physikalisch-Technischen-Reichsanstalt, liquefaction of H₂ (20K)

7.3.1925 first liquefaction of He in Germany (4.2 K, 200 ml), 3rd system world-wide besides Leiden and Toronto

1933 discovery of perfect diamagnetism of superconductors together with Ochsenfeld
→ **Meißner-Ochsenfeld Effect**

1934 offer of chair at the Technische Hochschule München (now TUM)

1946 – 1950 president of the Bavarian Academy of Sciences and Humanities

1946 foundation of the commission for Low Temperature Research
→ **Walther-Meißner-Institut**



Walther Meißner

* 16. Dezember 1882 in Berlin
† 15. November 1974 in Munich

Walther Meißner - der Mann, mit dem die Kälte kam
W. Buck, D. Einzel, R. Gross, Physik Journal, Mai 2013

Low Temperature Physics

at

WMI

Low Temperature Physics at WMI

- **superconductivity and superfluidity**
- **magnetism and spintronics**
- **nanoscale superconducting and spintronic devices**
- **solid-state based quantum systems**
- **superconducting quantum circuits for quantum computing**
- **quantum microwave communication and sensing**
-

an appetizer

Low Temperature Physics at WMI

innovative cryoengineering



Oxford Instruments Triton family

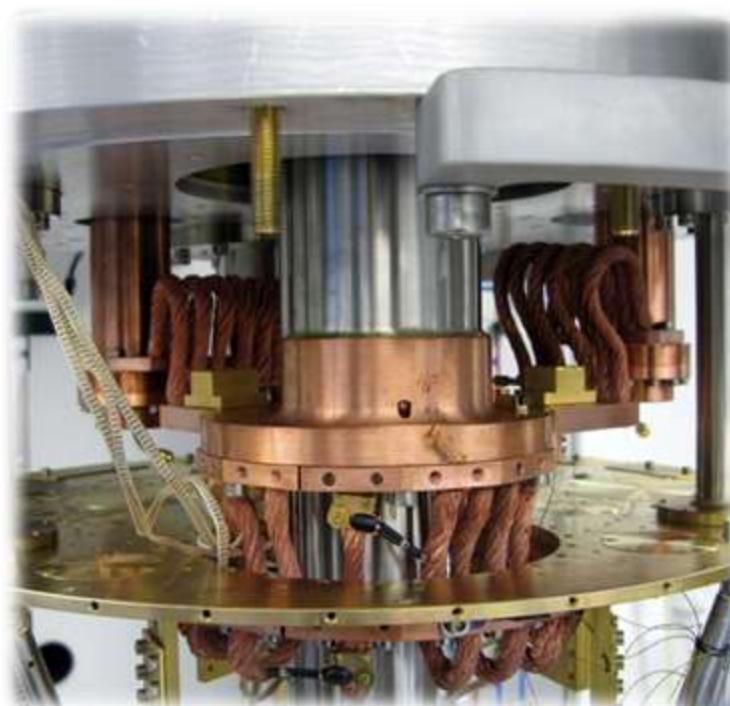
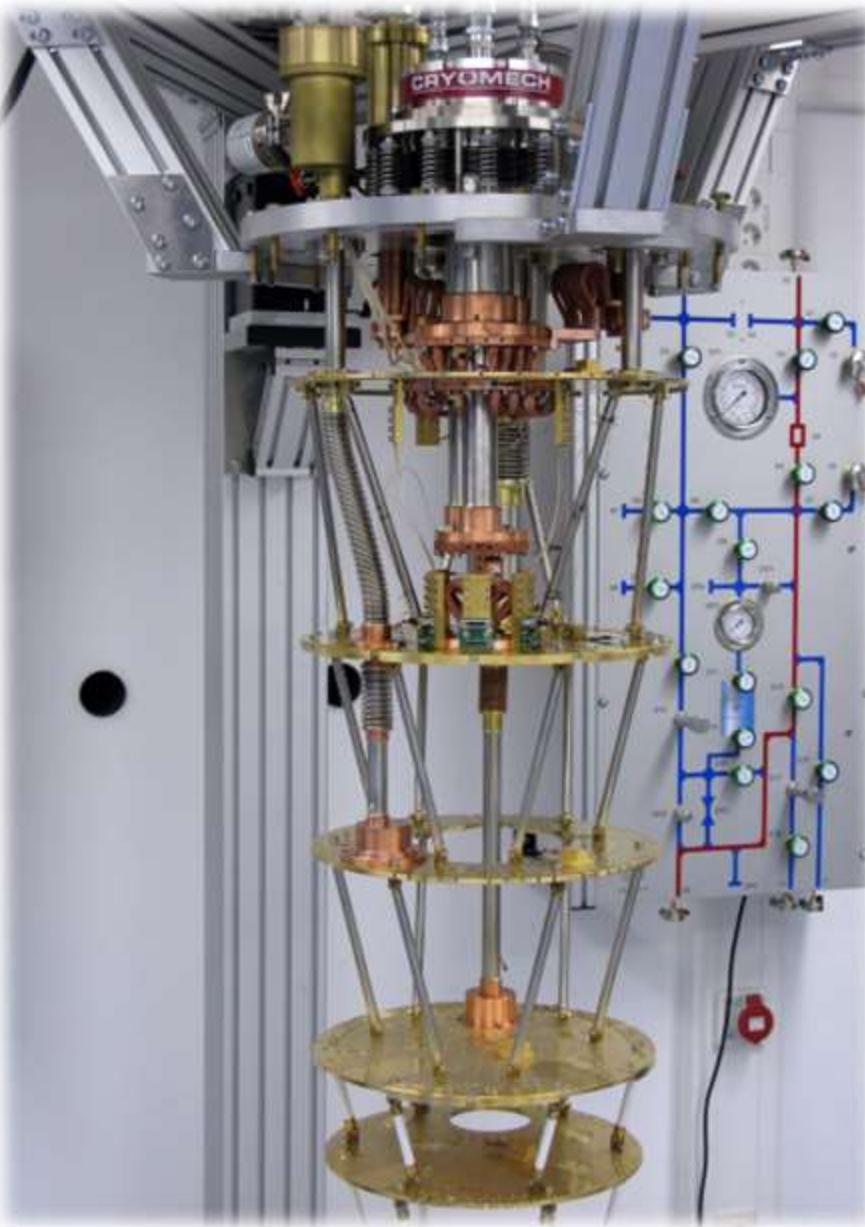
market share of dry dilution fridges: > 95 %

.....*WMI develops first dry dilution fridge*

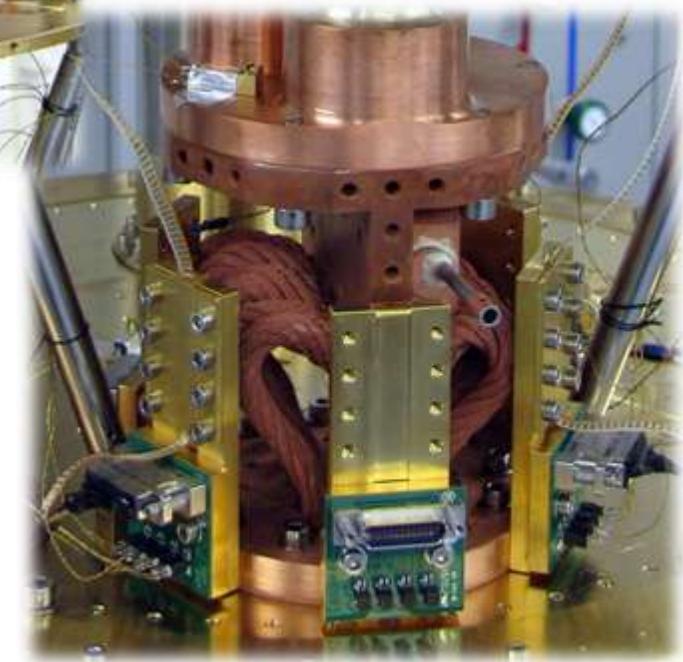
K. Uhlig, Cryogenics 42, 73 – 77 (2002)



Low Temperature Physics at WMI



*dry dilution fridge
designed and fabricated
at WMI*



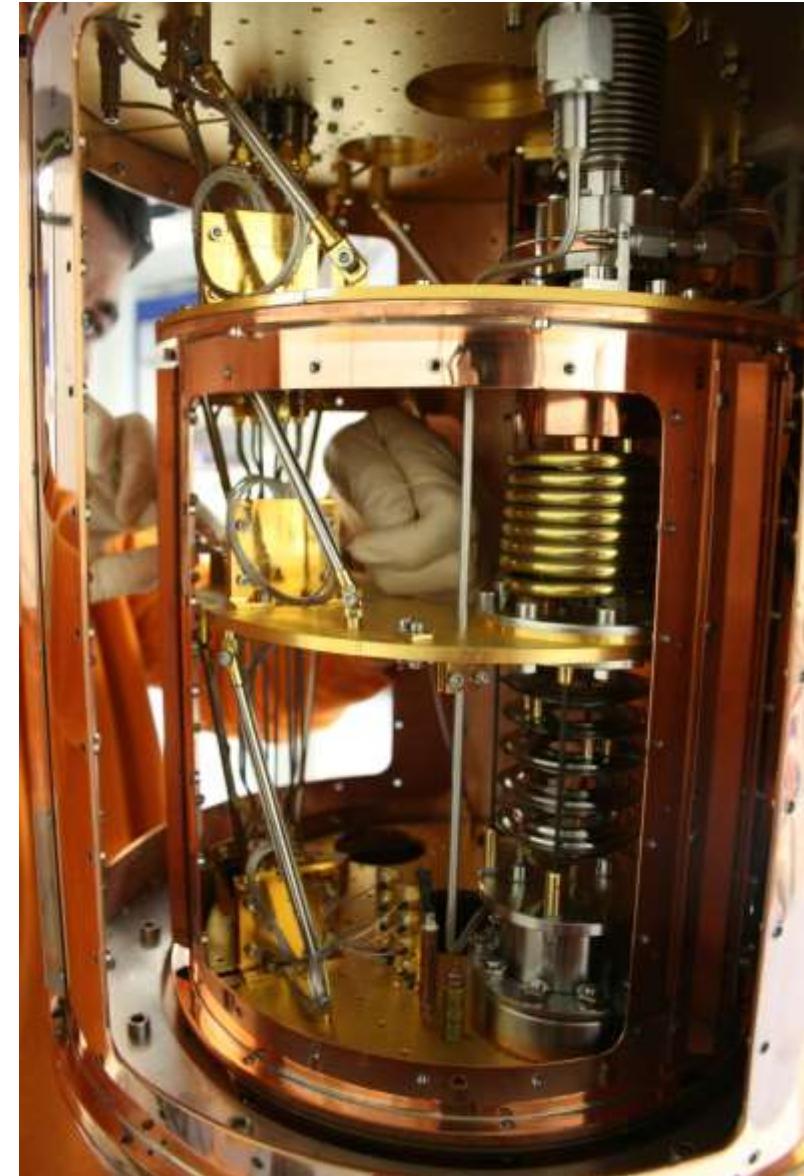
Low Temperature Physics at WMI

- BlueFors XLD Dilution Fridge (2020)



Low Temperature Physics at WMI

- Oxford Instruments Dilution Fridge (2011)
(with 3D vector magnet)

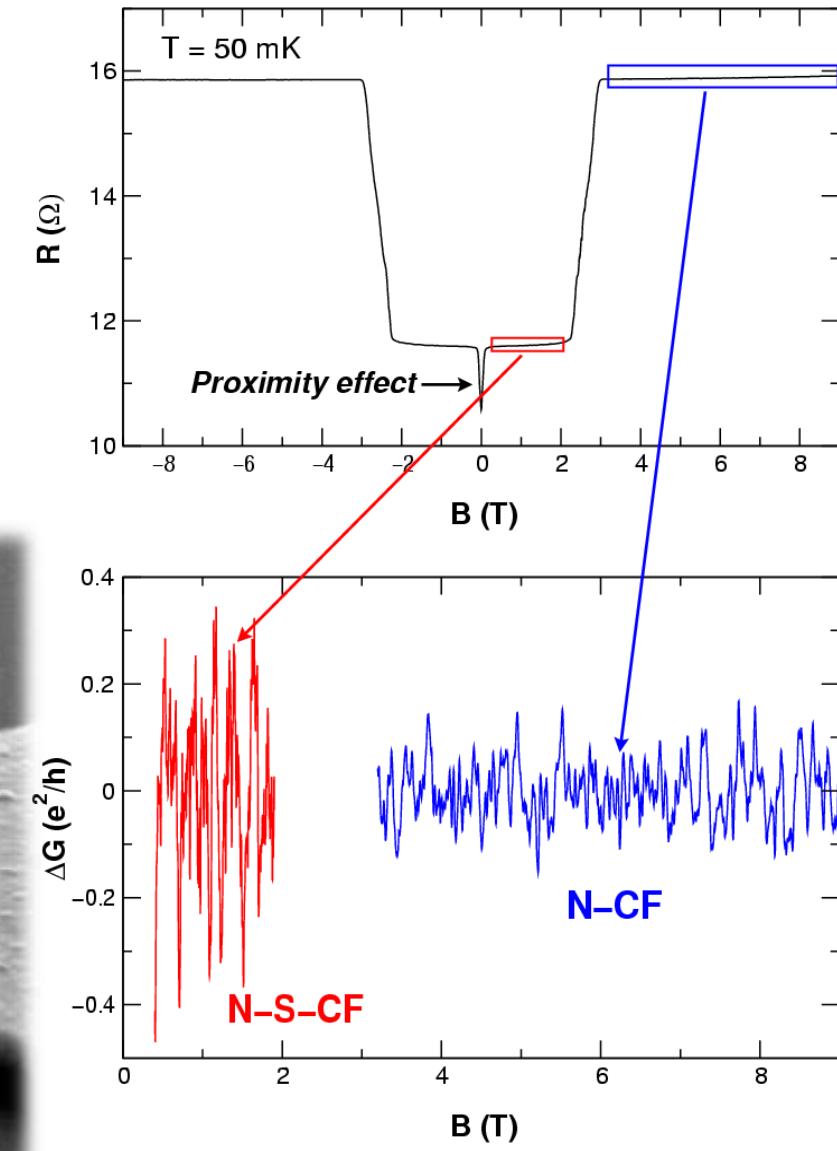
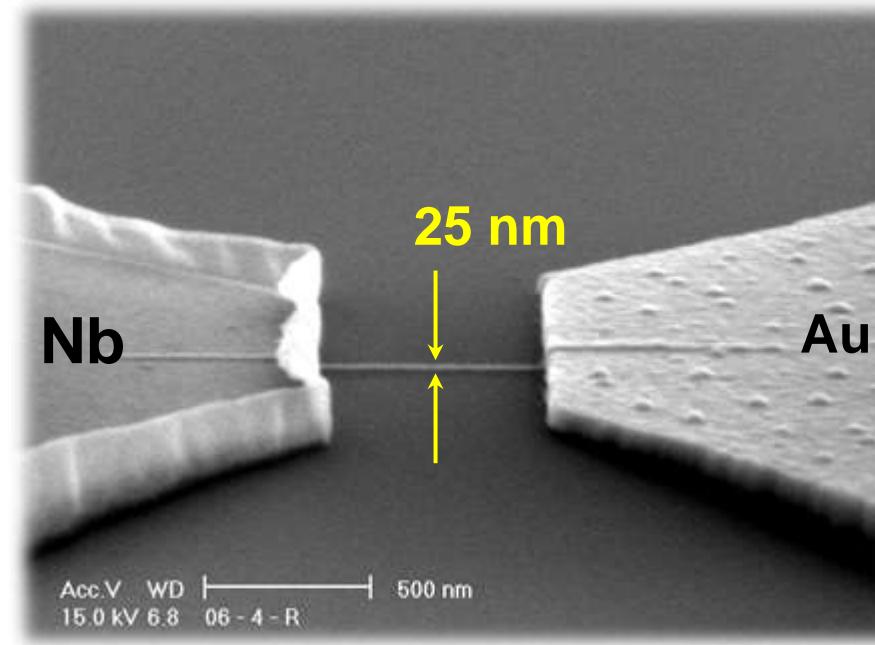
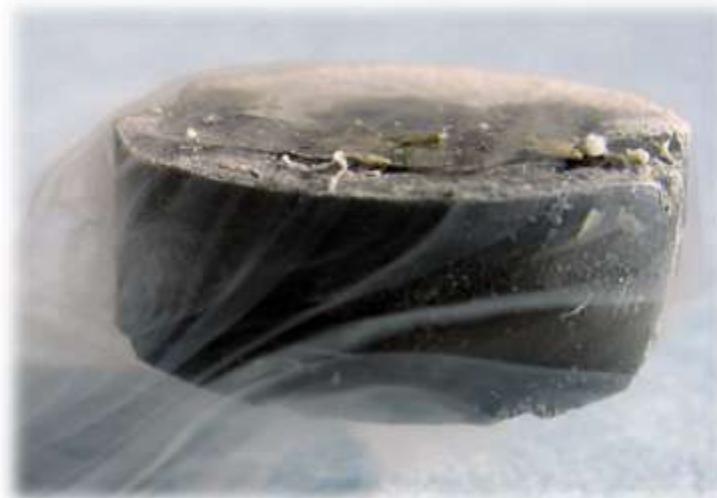


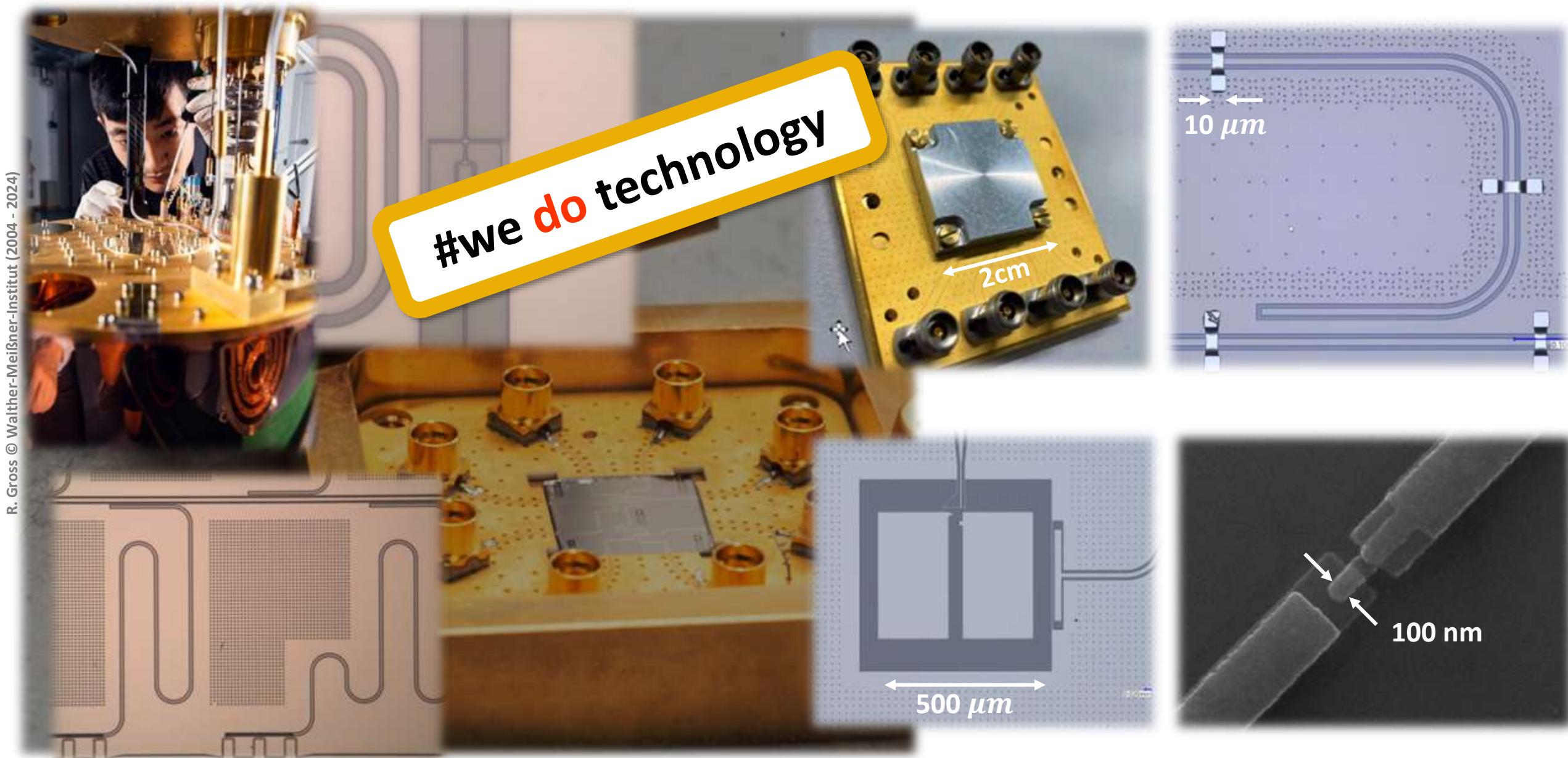
Helium Liquefaction

- *Helium liquefier at WMI:*
Linde TCF 20
- *supply of LHe to both Munich
Universities*
- *liquefaction power:*
 $> 150\,000 \text{ l/year}$
- *market price:*
about 4 Mio. €



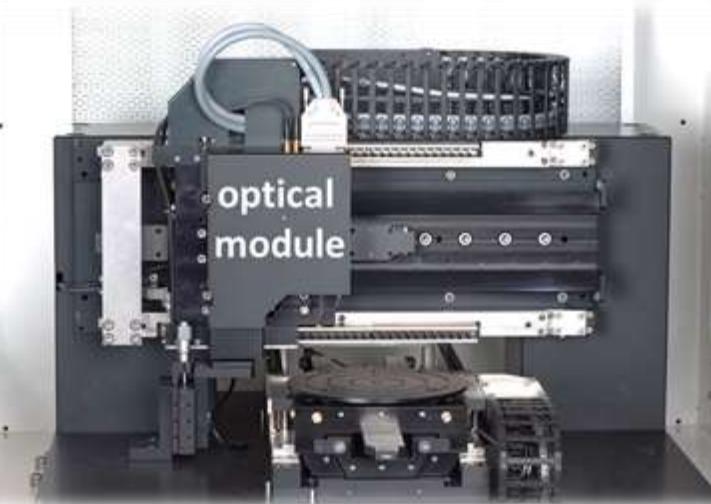
Low Temperature Physics at WMI



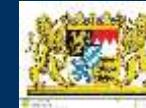


Hub for Nano-, Thin Film and Cryotechnology

R. Gross © Walther-Meißner-Institut (2004 - 2024)



Quantum Technology Projects @ WMI



Bayerisches Staatsministerium
für Wissenschaft und Kunst

GeQCoS (BMBF)
MQV-SQQC (StMWK Bayern)
MUNIQC-SC (BMBF)



Bundesministerium
für Bildung
und Forschung



BUILDING
**QUANTUM
COMPUTERS**

Demonstrator-QC → NISQ-QC → FT-QC
~ 10 Qubits ~ 100 Qubits ~ 10^6 Qubits



Have
Fun !!